

# Looking for seams



15-463, 15-663, 15-862  
Computational Photography  
Fall 2017, Lecture 8

# Course announcements

- Apologies for canceling Monday's lecture.
- Homework 3 will be posted tonight.
  - Due October 12th.
- Comments on Homework 2?

# Overview of today's lecture

- Back to cutting-and-pasting (and other motivating examples).
- Image as a graph.
- Shortest graph paths and Intelligent scissors.
- Graph-cuts and GrabCut.
- Some notes about cutting-and-pasting.

# Slide credits

Most of these slides were adapted from:

- Kris Kitani (15-463, Fall 2016).

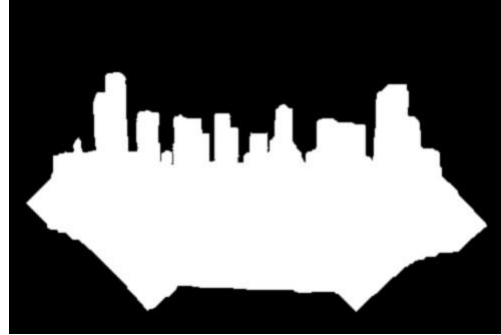
Some slides were inspired or taken from:

- Fredo Durand (MIT).
- James Hays (Georgia Tech).

Back to cutting-and-pasting (and other motivating examples)

# Cut and paste procedure

## 1. Extract Sprites



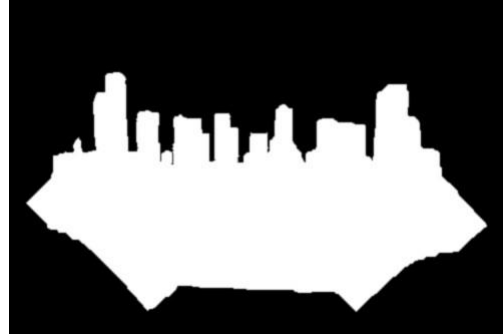
## 2. Blend them into the composite





# Cut and paste procedure

## 1. Extract Sprites



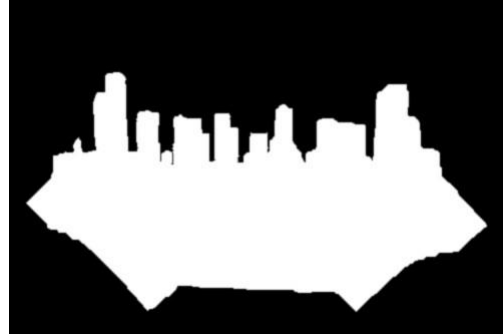
## 2. Blend them into the composite



How do we do this?

# Cut and paste procedure

## 1. Extract Sprites



How do we do this?

Two different ways to think about the same thing:

- Finding seams (i.e., finding the pixels where to cut an image)
- Segmentation (i.e., splitting the image into “foreground” and “background”)

I will be using the two terms interchangeable



# Applications

Finding seams is also useful for:

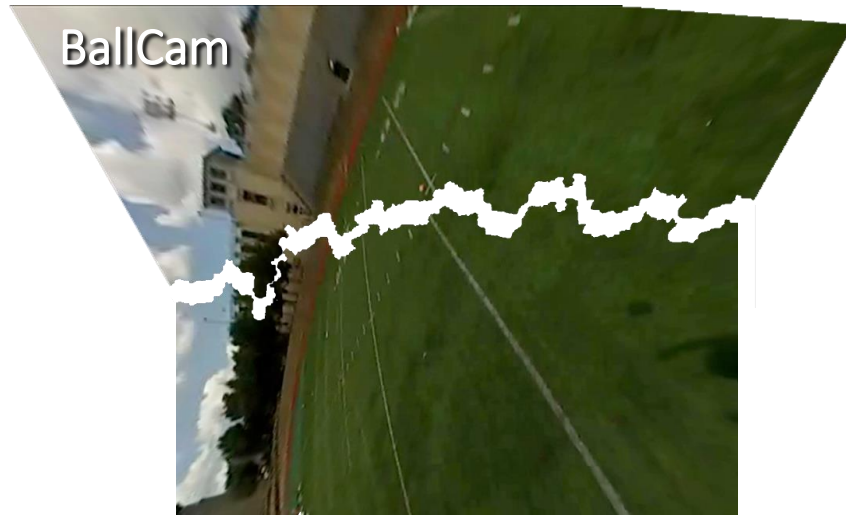


image stitching



retargeting

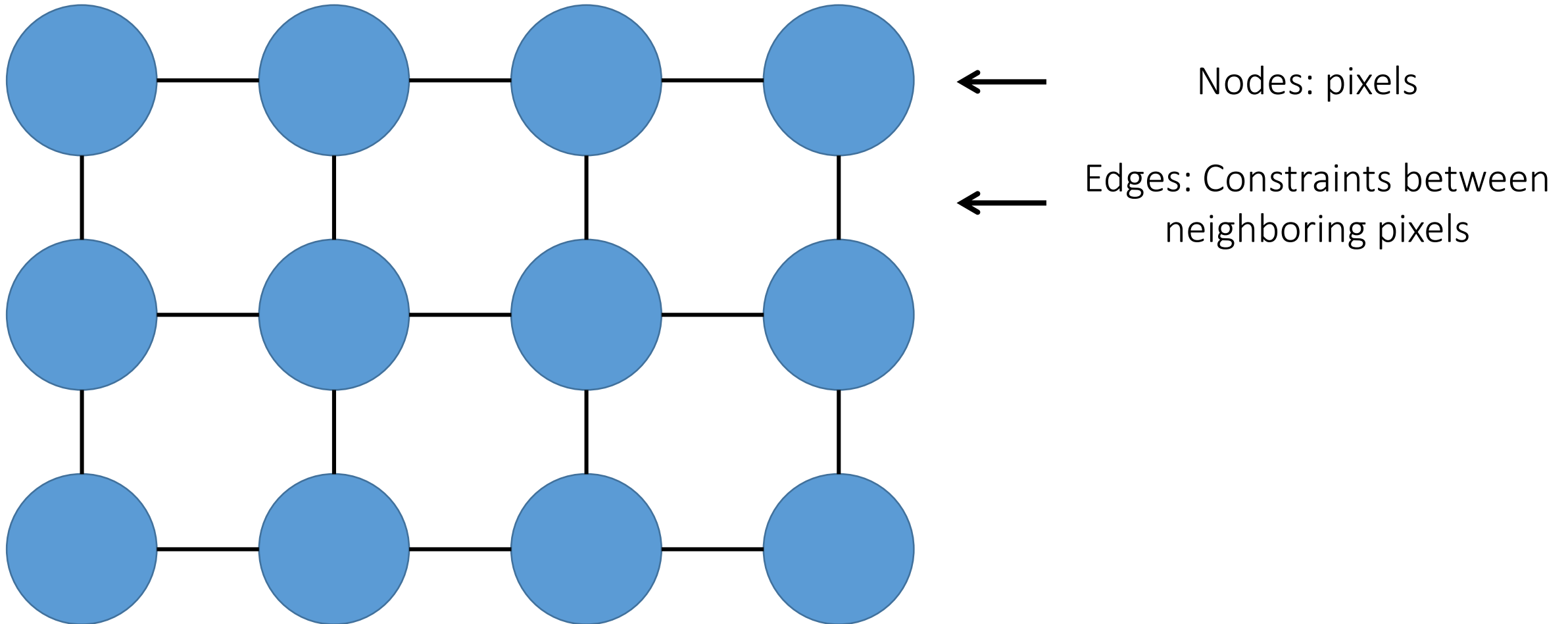


segmentation

Image as a graph

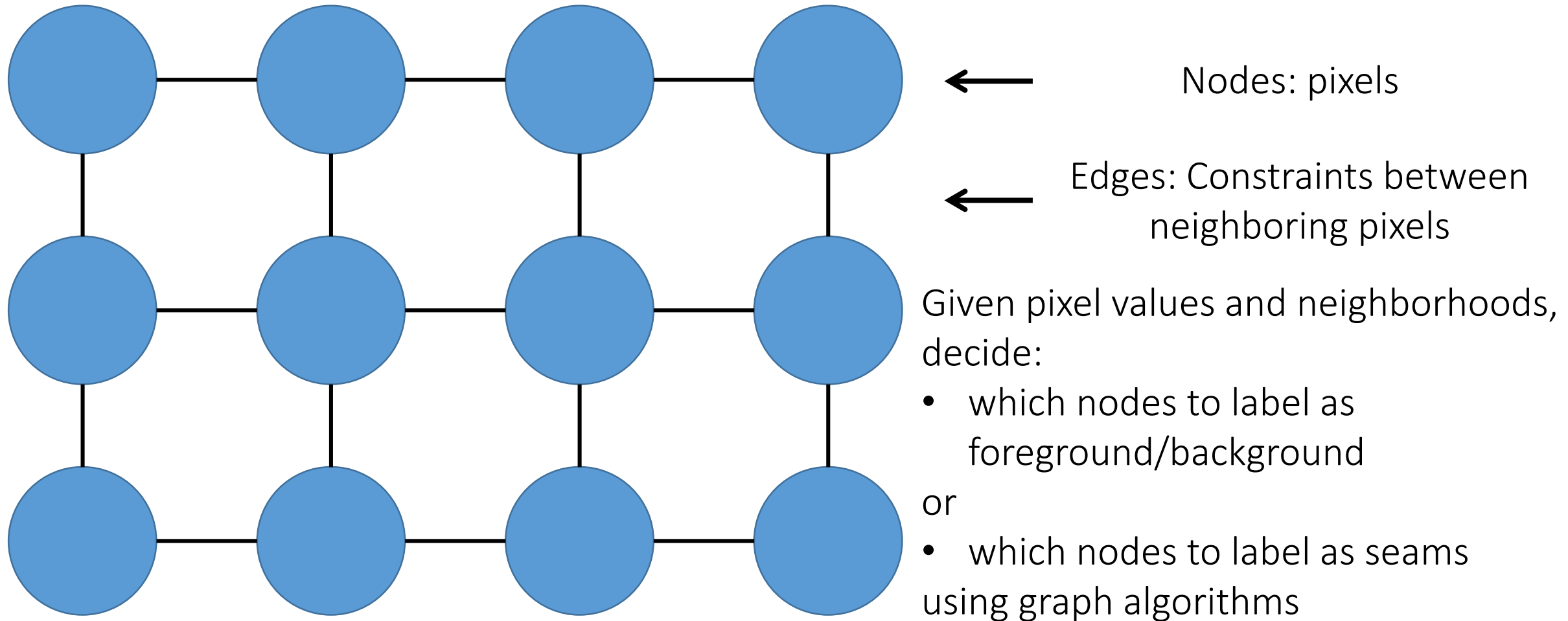
# Fundamental theme of today's lecture

Images can be viewed as graphs



# Graph-view of segmentation problem

Segmentation is node-labeling



# Graph-view of segmentation problem

Today we will cover:

Method	Labeling problem	Algorithm	Intuition
<b>Intelligent scissors</b>	label pixels as seams	Dijkstra's shortest path (dynamic programming)	short path is a good <b>boundary</b>
<b>GrabCut</b>	label pixels as foreground/background	max-flow/min-cut (graph cutting)	good <b>region</b> has low cutting cost

Shortest graph paths and intelligent scissors



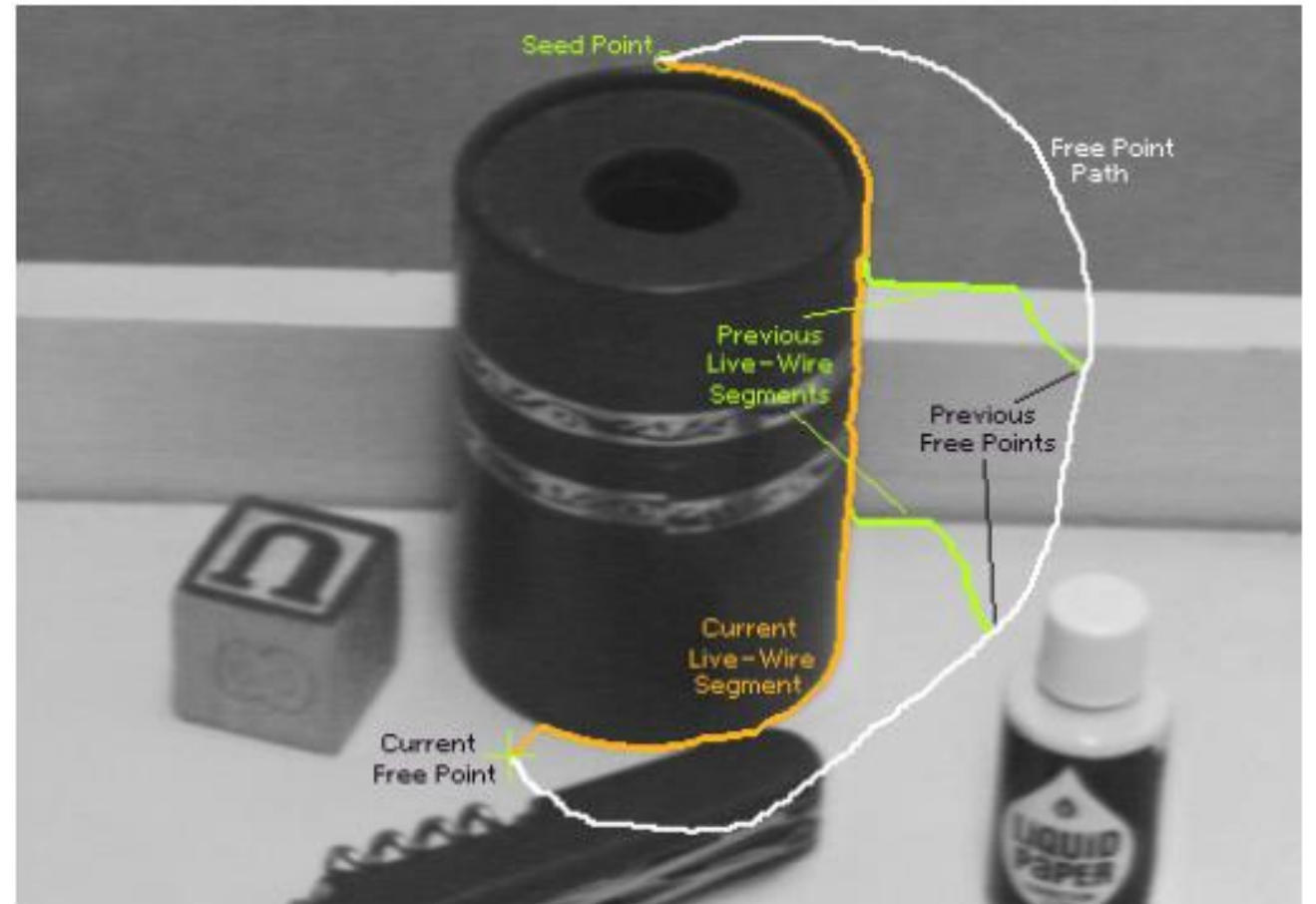
# Intelligent scissors

Problem statement:

Given two seed points, find a good boundary connecting them

Challenges:

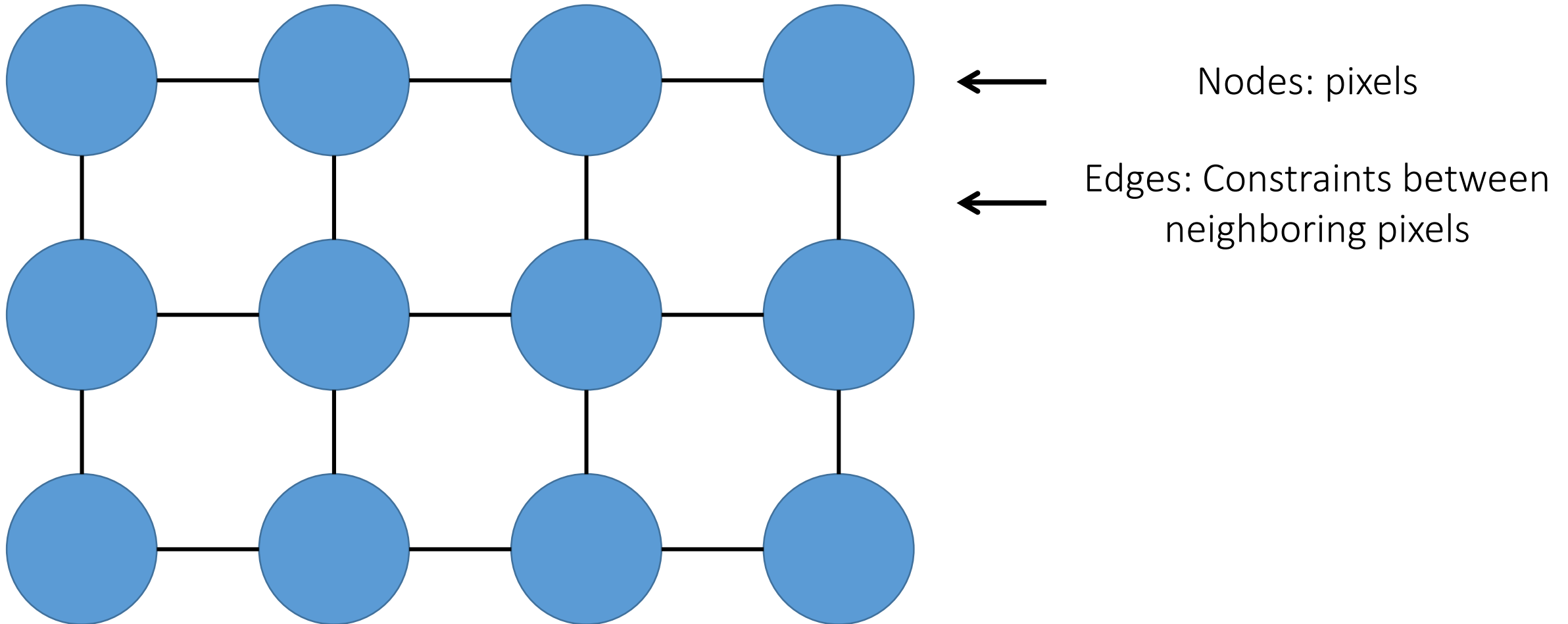
- Make this real-time for interaction
- Define what makes a good boundary



Mortenson and Barrett (SIGGRAPH 1995)  
(you can tell it's old from the paper's low quality teaser figure)

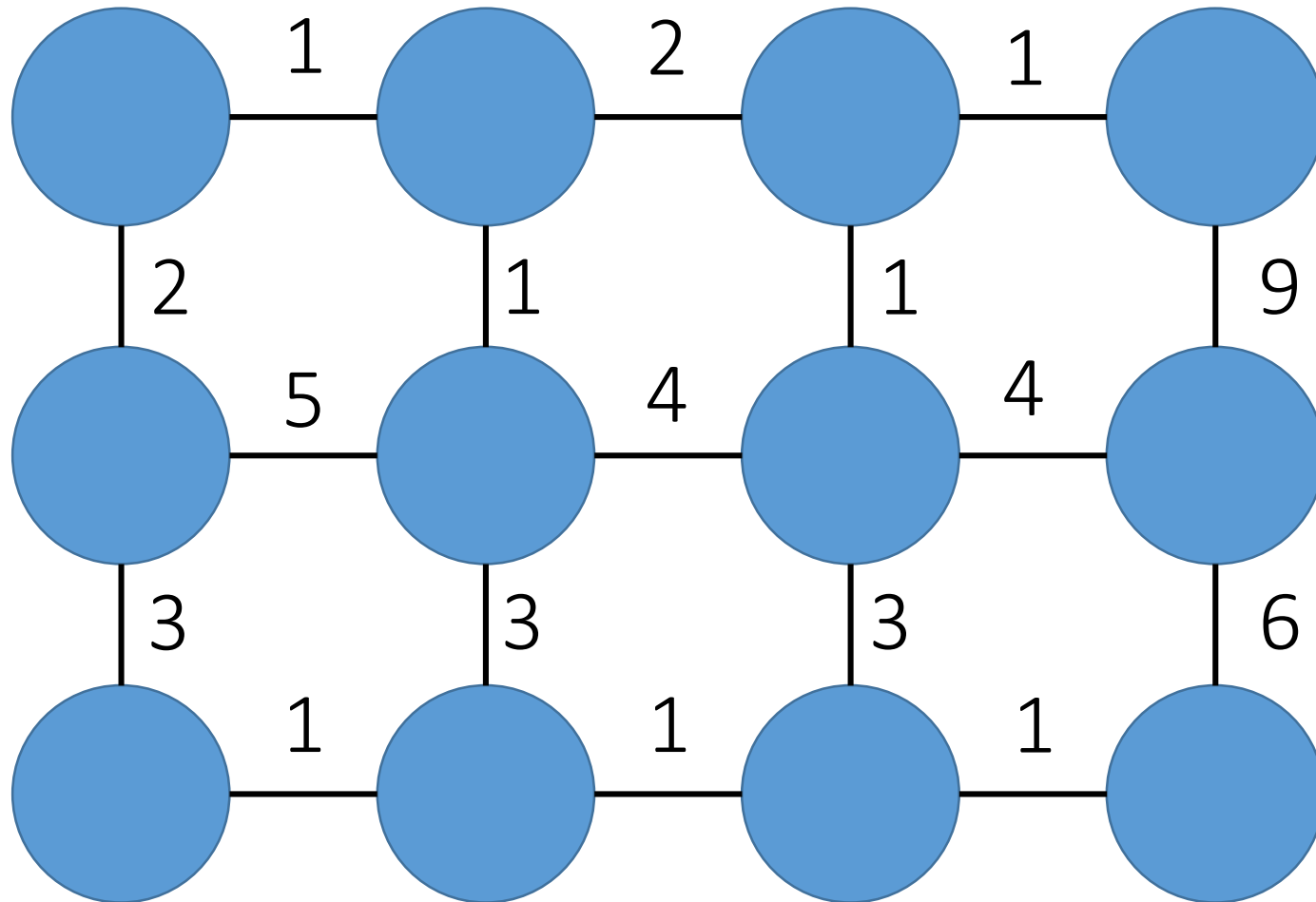
# Graph-view of this problem

Images can be viewed as graphs



# Graph-view of this problem

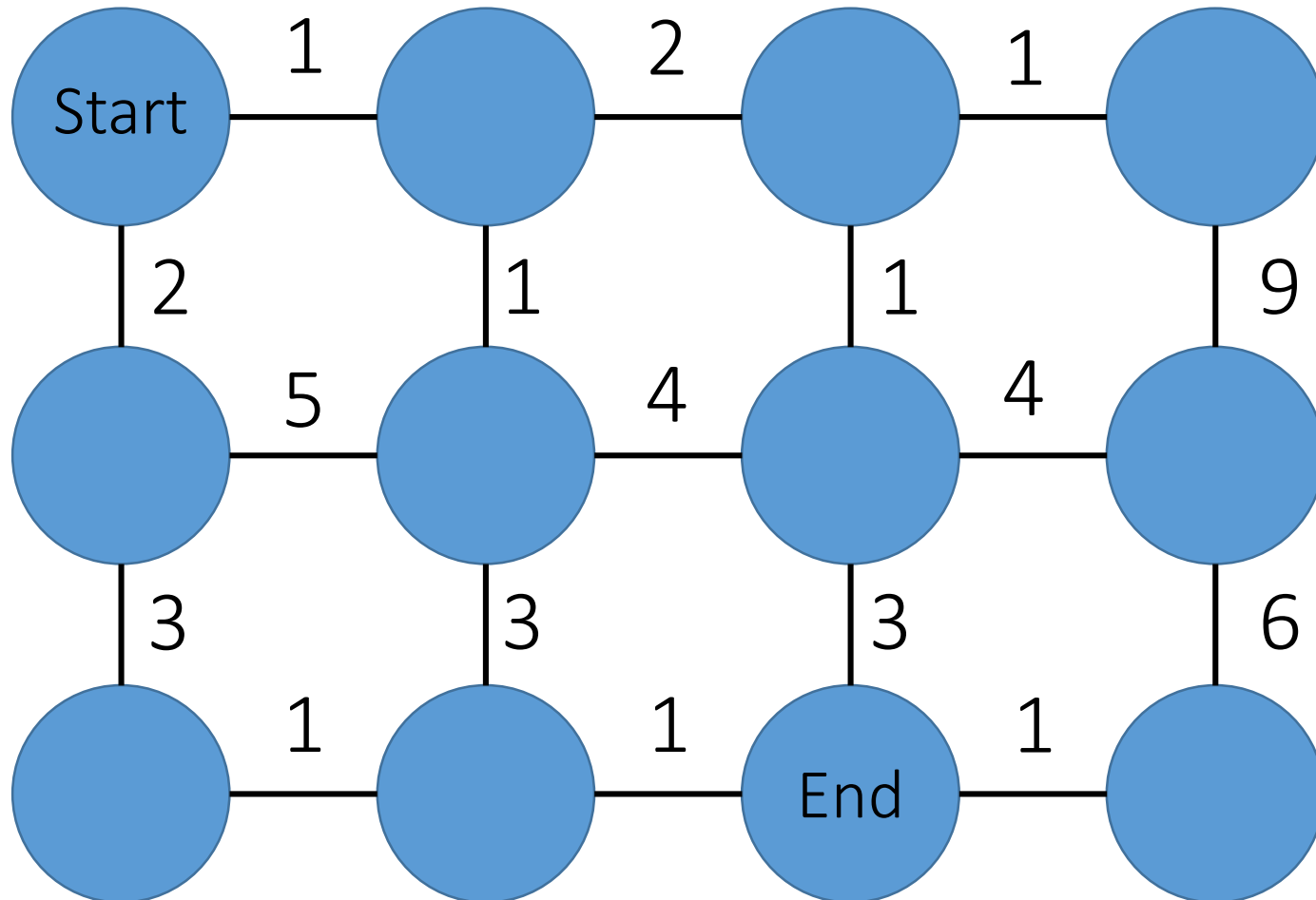
Graph-view of intelligent scissors:



1. Assign weights (costs) to edges

# Graph-view of this problem

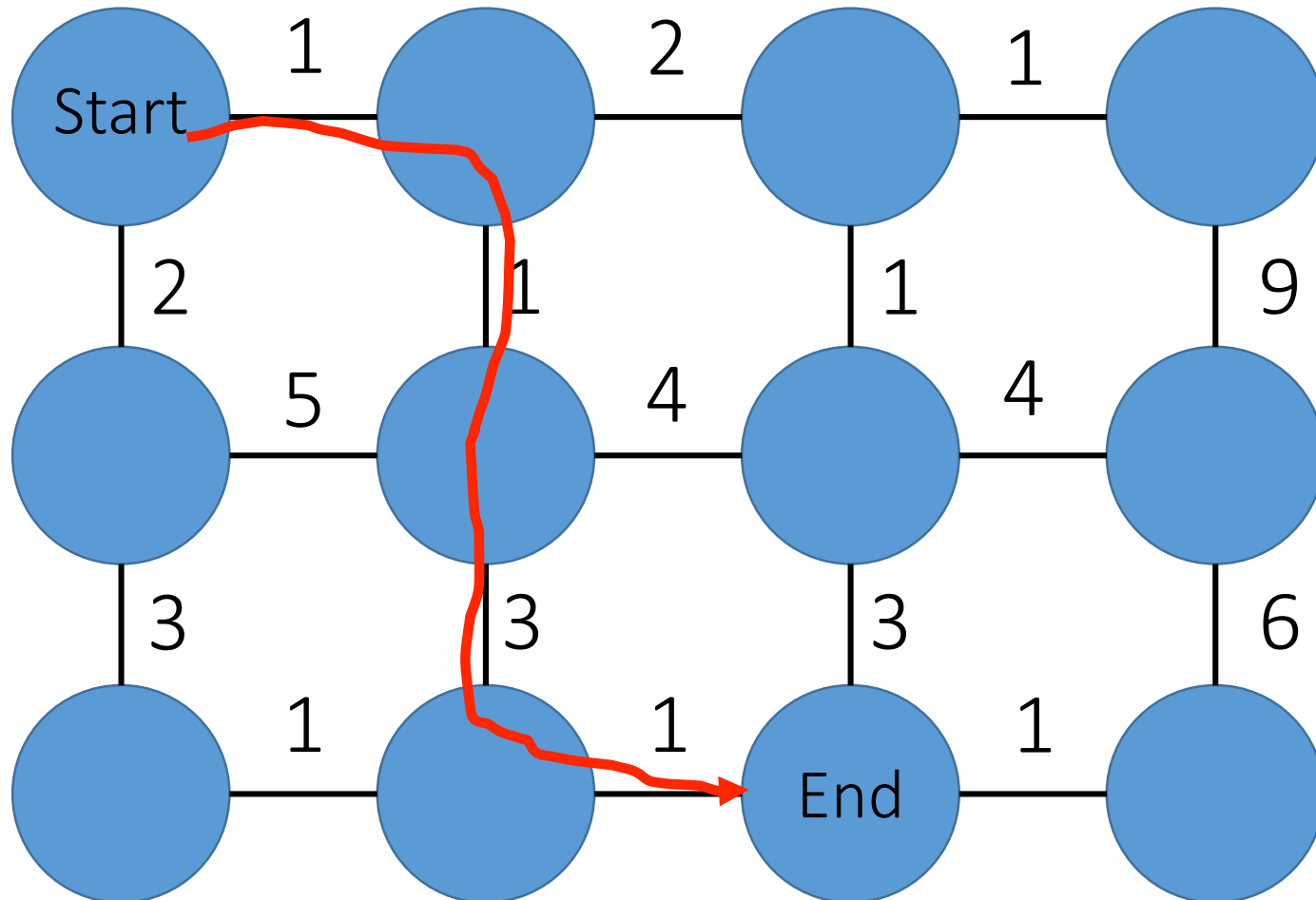
Graph-view of intelligent scissors:



1. Assign weights (costs) to edges
2. Select the seed nodes

# Graph-view of this problem

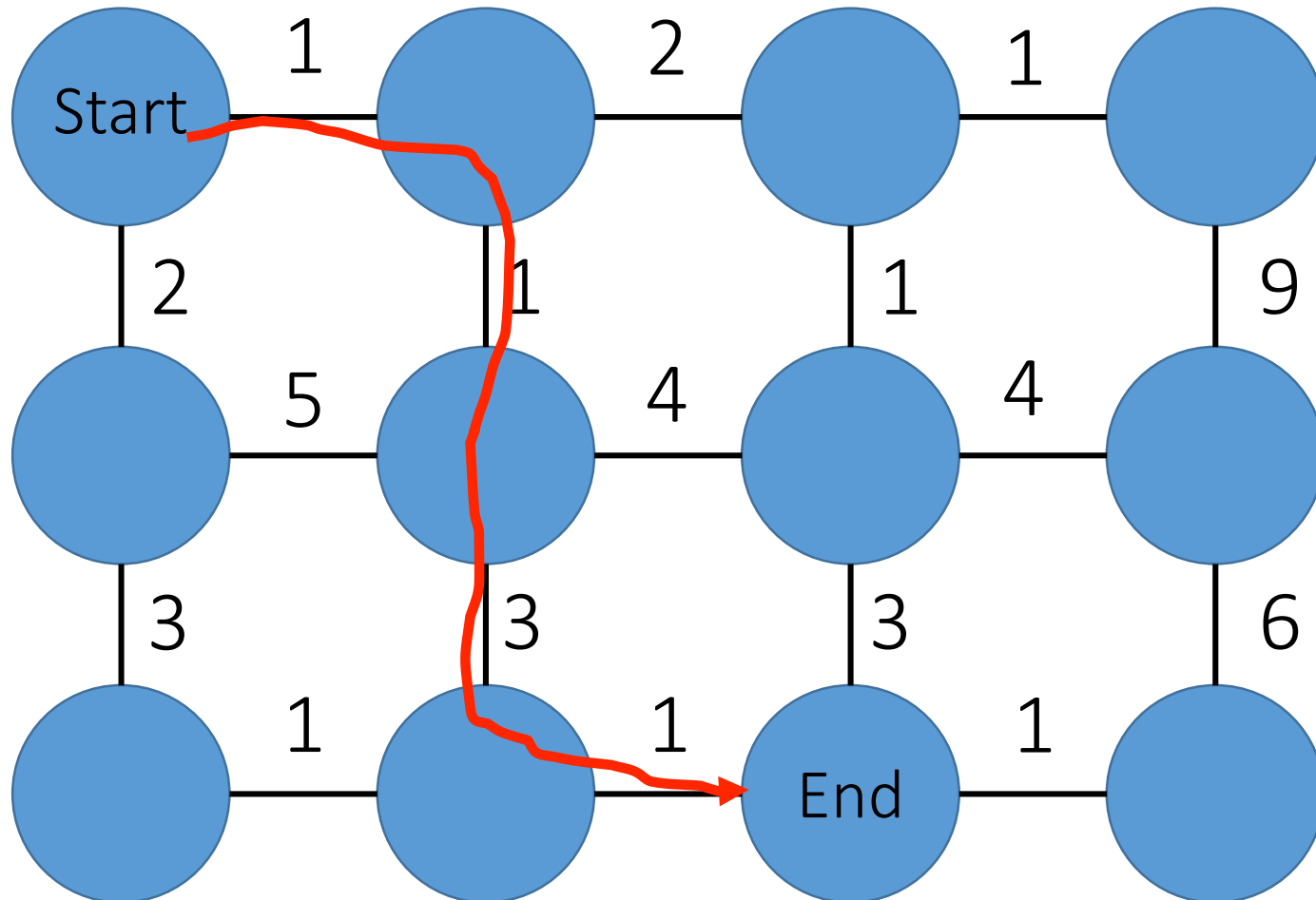
Graph-view of intelligent scissors:



1. Assign weights (costs) to edges
2. Select the seed nodes
3. Find shortest path between them

# Graph-view of this problem

Graph-view of intelligent scissors:



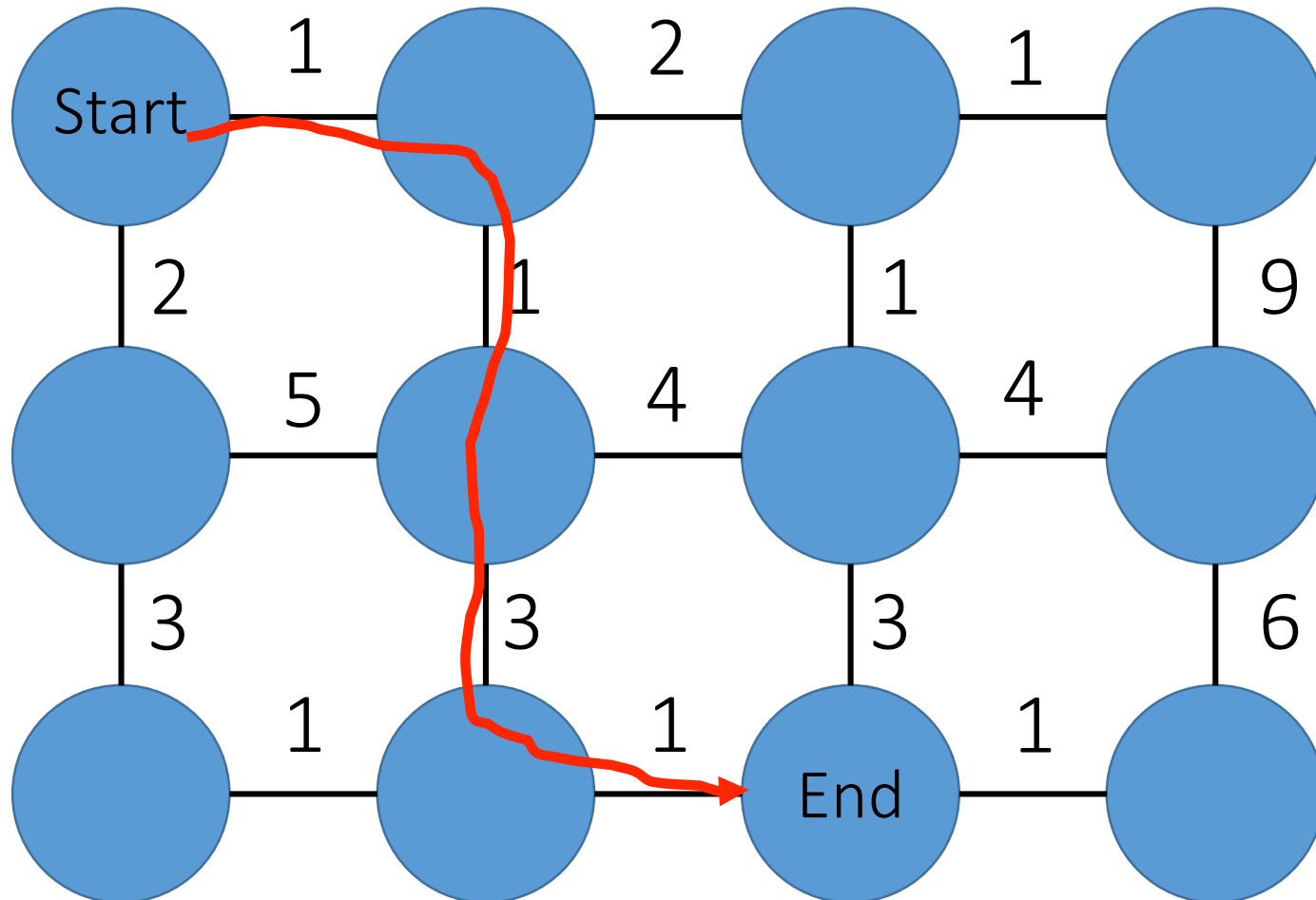
1. Assign weights (costs) to edges
2. Select the seed nodes
3. Find shortest path between them

What algorithm can we use to find the shortest path?



# Graph-view of this problem

Graph-view of intelligent scissors:



1. Assign weights (costs) to edges
2. Select the seed nodes
3. Find shortest path between them

What algorithm can we use to find the shortest path?

- Dijkstra's algorithm (dynamic programming)

# Dijkstra's shortest path algorithm

**Initialize**, given seed  $s$  (*pixel ID*):

- $\text{cost}(s) = 0$                       % total cost from seed to this point
- $\text{cost}(!s) = \text{big}$
- $\mathbf{A} = \{\text{all pixels}\}$               % set to be expanded
- $\text{prev}(s) = \text{undefined}$           % pointer to pixel that leads to  $q=s$

Precompute  $\text{cost}_2(q, r)$     % cost between  $q$  to neighboring pixel  $r$

**Loop** while  $\mathbf{A}$  is not empty

1.  $q$  = pixel in  $\mathbf{A}$  with lowest cost

2. Remove  $q$  from  $\mathbf{A}$

3. For each pixel  $r$  in neighborhood of  $q$  that is in  $\mathbf{A}$

    a)  $\text{cost\_tmp} = \text{cost}(q) + \text{cost}_2(q, r)$  %this updates the costs

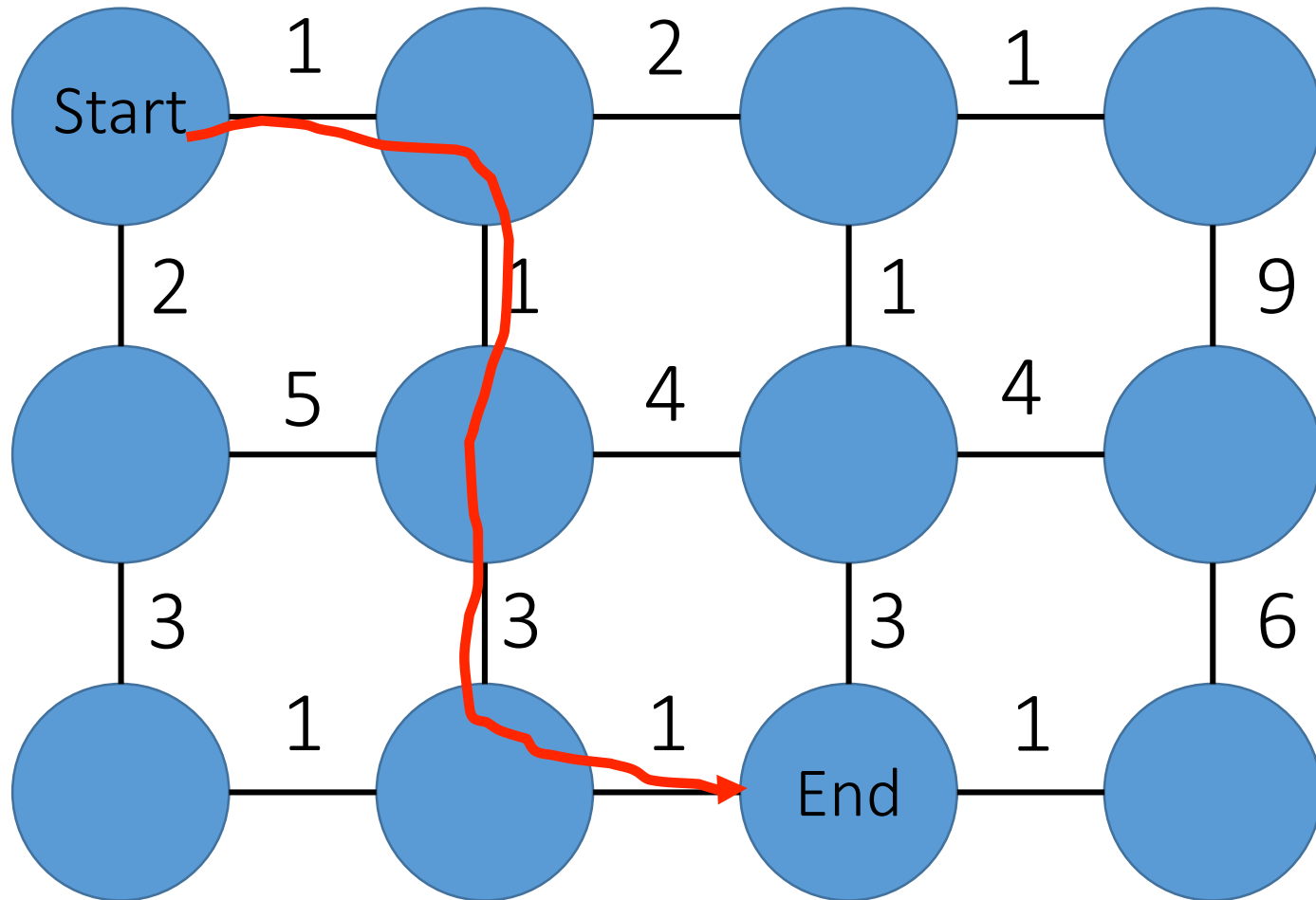
    b) if ( $\text{cost\_tmp} < \text{cost}(r)$ )

        i.  $\text{cost}(r) = \text{cost\_tmp}$

        ii.  $\text{prev}(r) = q$

# Graph-view of this problem

Graph-view of intelligent scissors:



1. Assign weights (costs) to edges
2. Select the seed nodes
3. Find shortest path between them

What algorithm can we use to find the shortest path?

- Dijkstra's algorithm (dynamic programming)

How should we select the edge weights to get good boundaries?

# Selecting edge weights

Define boundary cost between neighboring pixels:

1. Lower if an image edge is present (e.g., as found by Sobel filtering).
2. Lower if the gradient magnitude at that point is strong.
3. Lower if gradient is similar in boundary direction.





# Selecting edge weights

Gradient magnitude

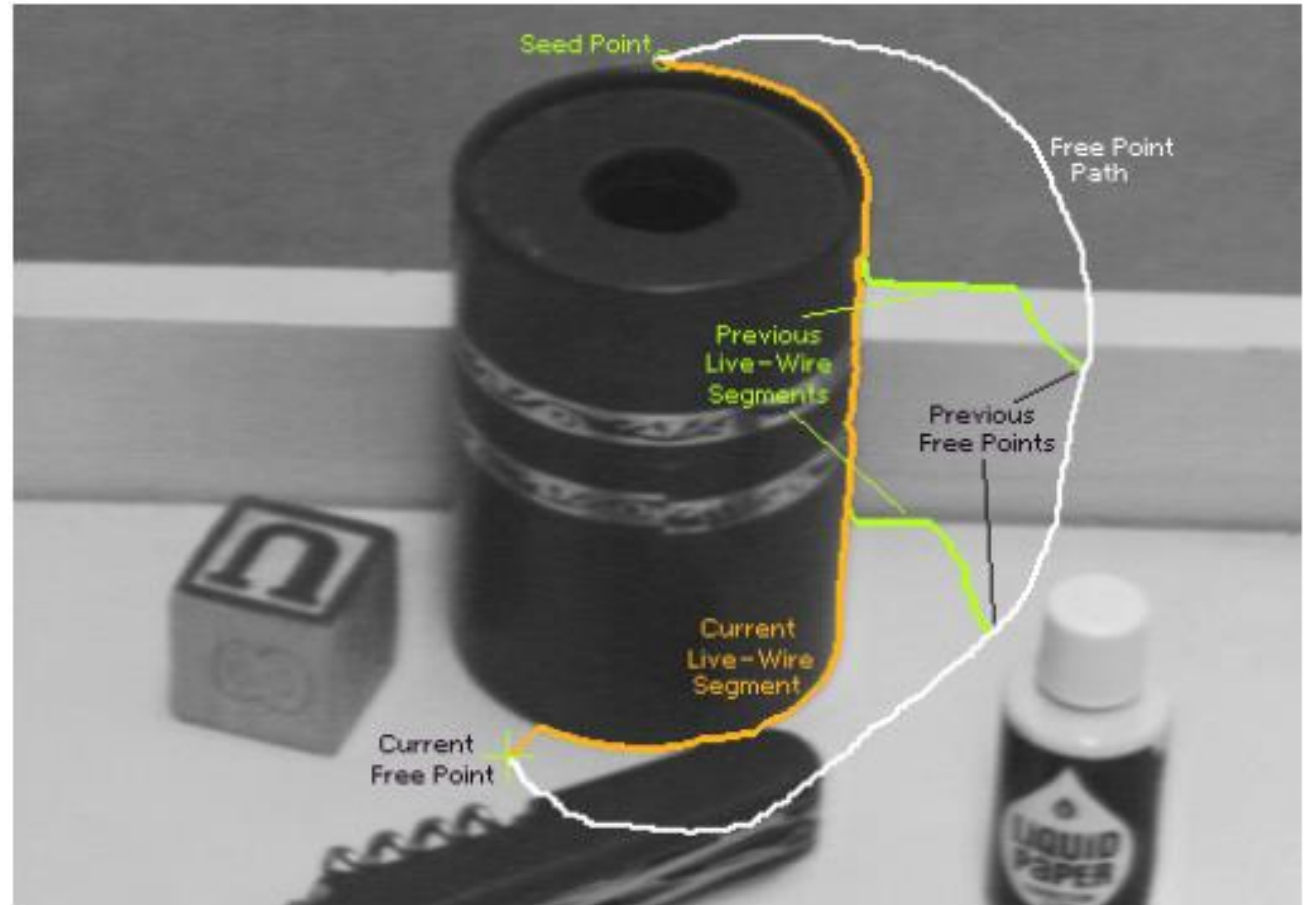


Pixel-wise cost

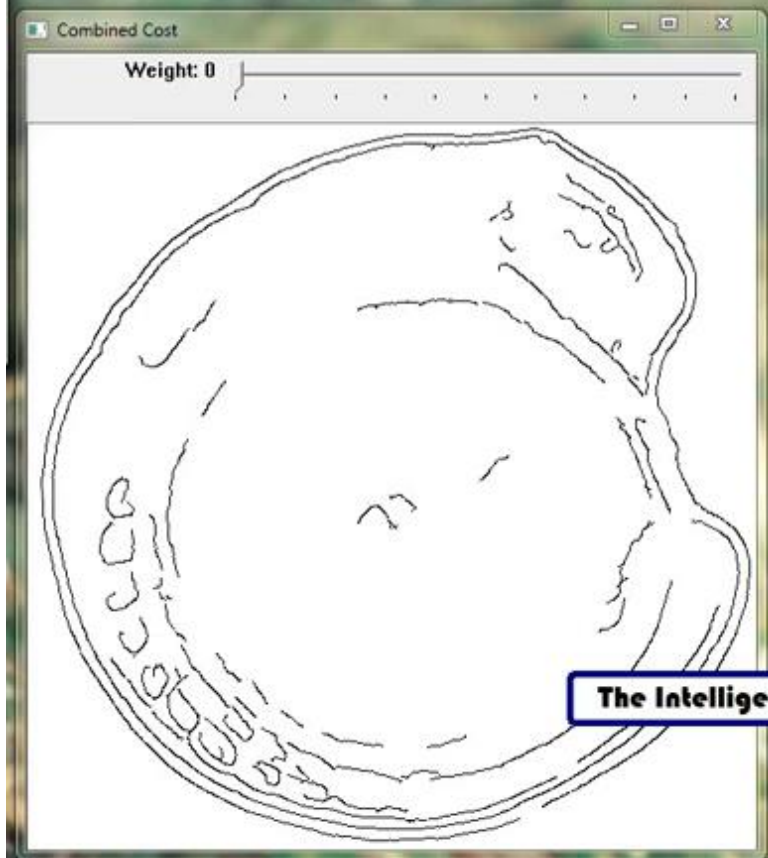
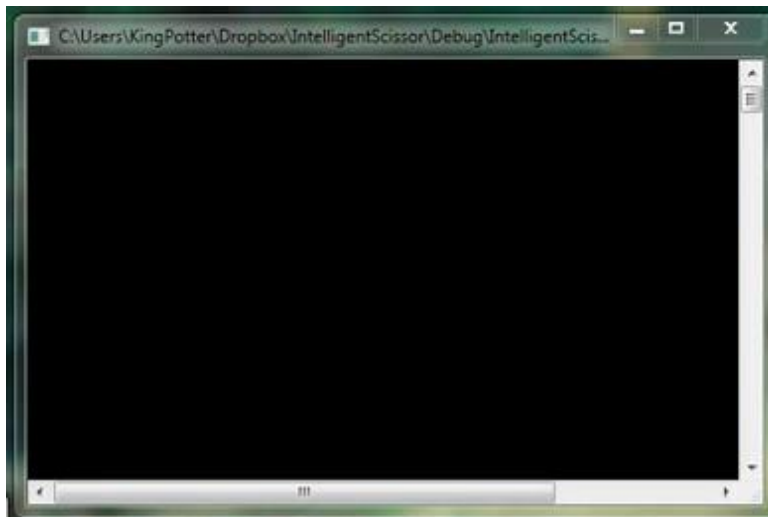
Edge image

# Making it more interactive

1. Use cursor as the “end” seed, and always connect start seed to that
2. Every time the user clicks, use that point as a new starting seed and repeat







**The Intelligent Scissor Demo**

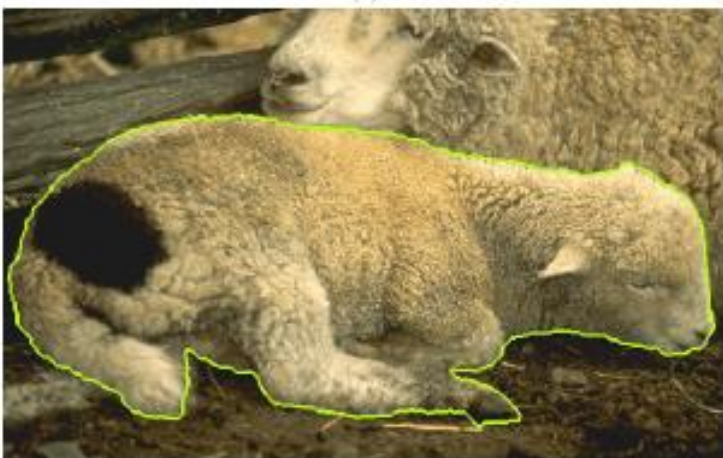
# Examples



(a)



(b)



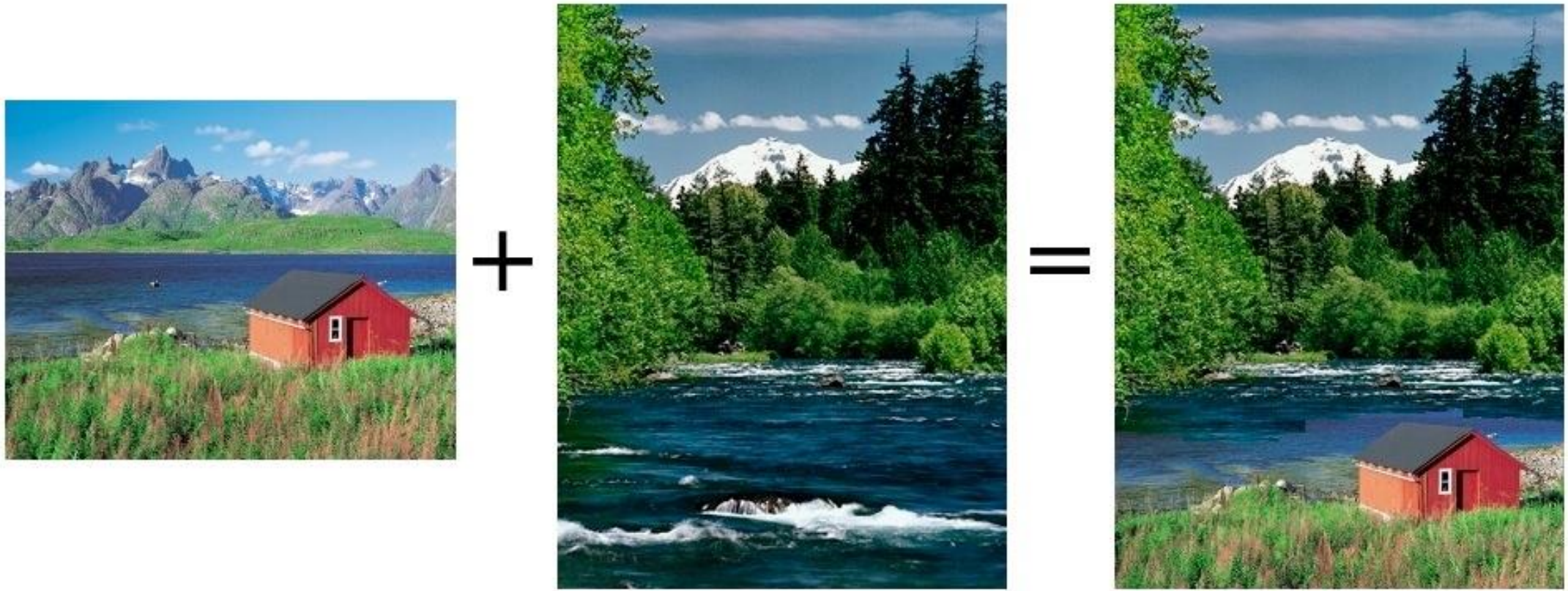
(c)





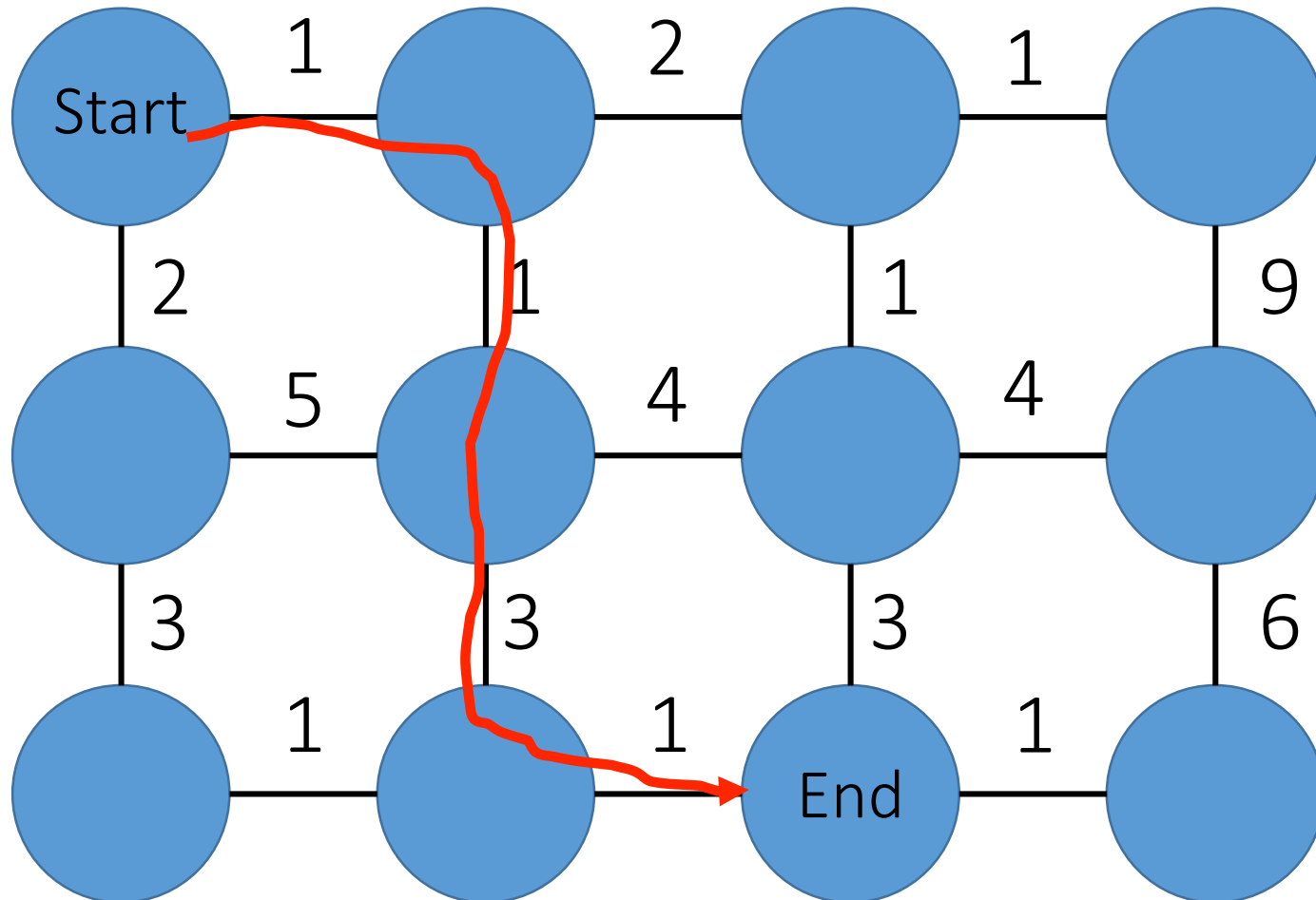
# Seam collaging

Another use for image seam selection



# Graph-view of this problem

Graph-view of image collaging:



1. Assign weights (costs) to edges
2. Select the seed nodes
3. Find shortest path between them

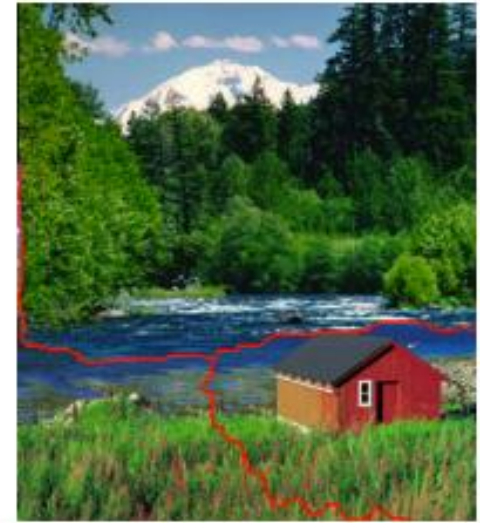
What edge weights would you use for collaging?



# Selecting edge weights for seam collaging

Good places to cut:

- similar color in both images
- high gradient in both images





# Seam carving

Another use for image seam selection

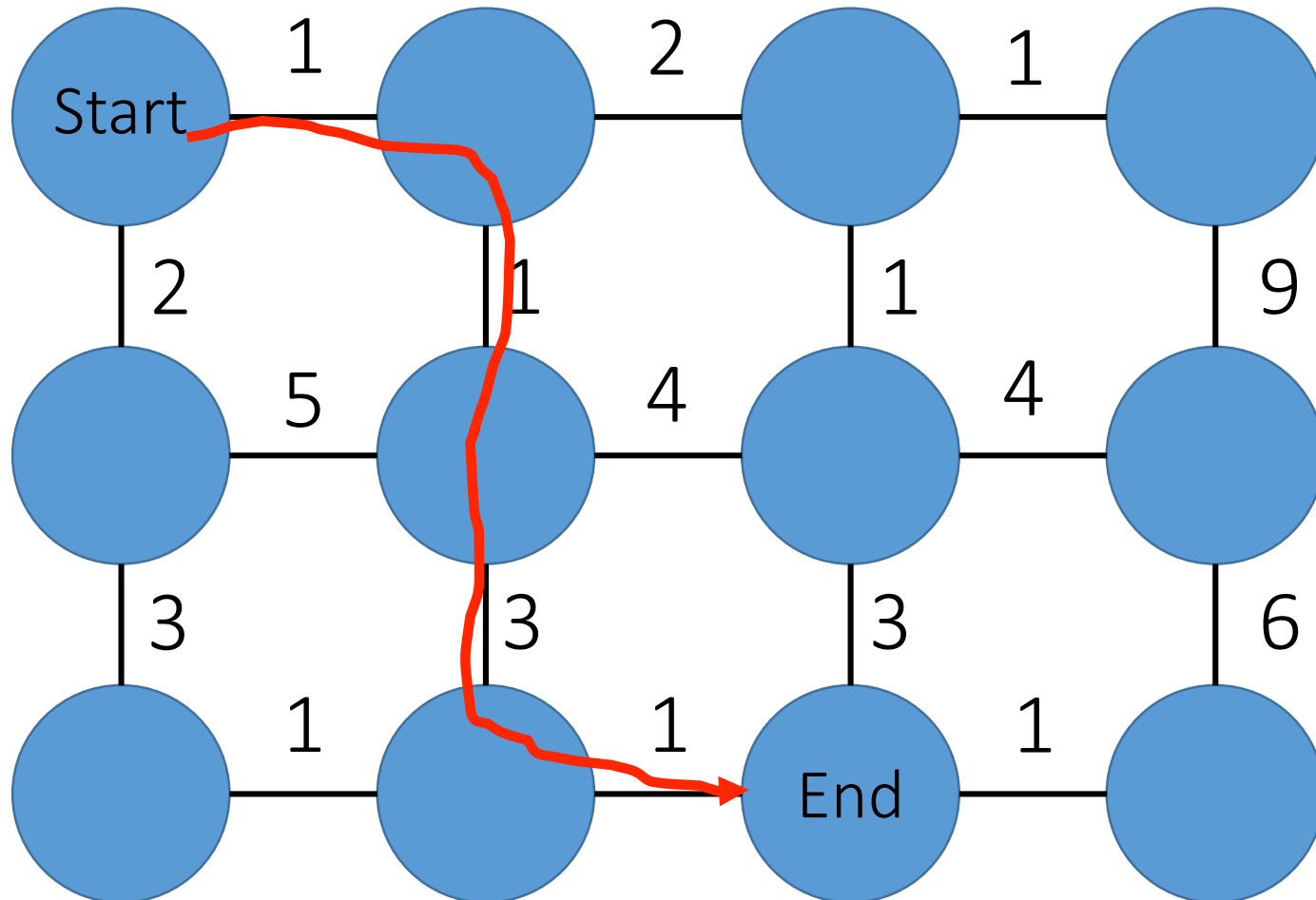


Avidan and Shamir, Seam Carving for Content-Aware Image Resizing, SIGGRAPH 2007



# Graph-view of this problem

Graph-view of seam carving:



1. Assign weights (costs) to edges
2. Select the seed nodes
3. Find shortest path between them

What edge weights would you use for seam carving?



Shai Avidan

Mitsubishi Electric Research Lab

Ariel Shamir

The interdisciplinary Center & MERL

# Question about blending (last lecture)

When blending multiple images of the same scene, moving objects become ghosts!



What can we do instead of blending?

# Question about blending (last lecture)

When blending multiple images of the same scene, moving objects become ghosts!



Instead of blending the images, cut them and stitch them together!



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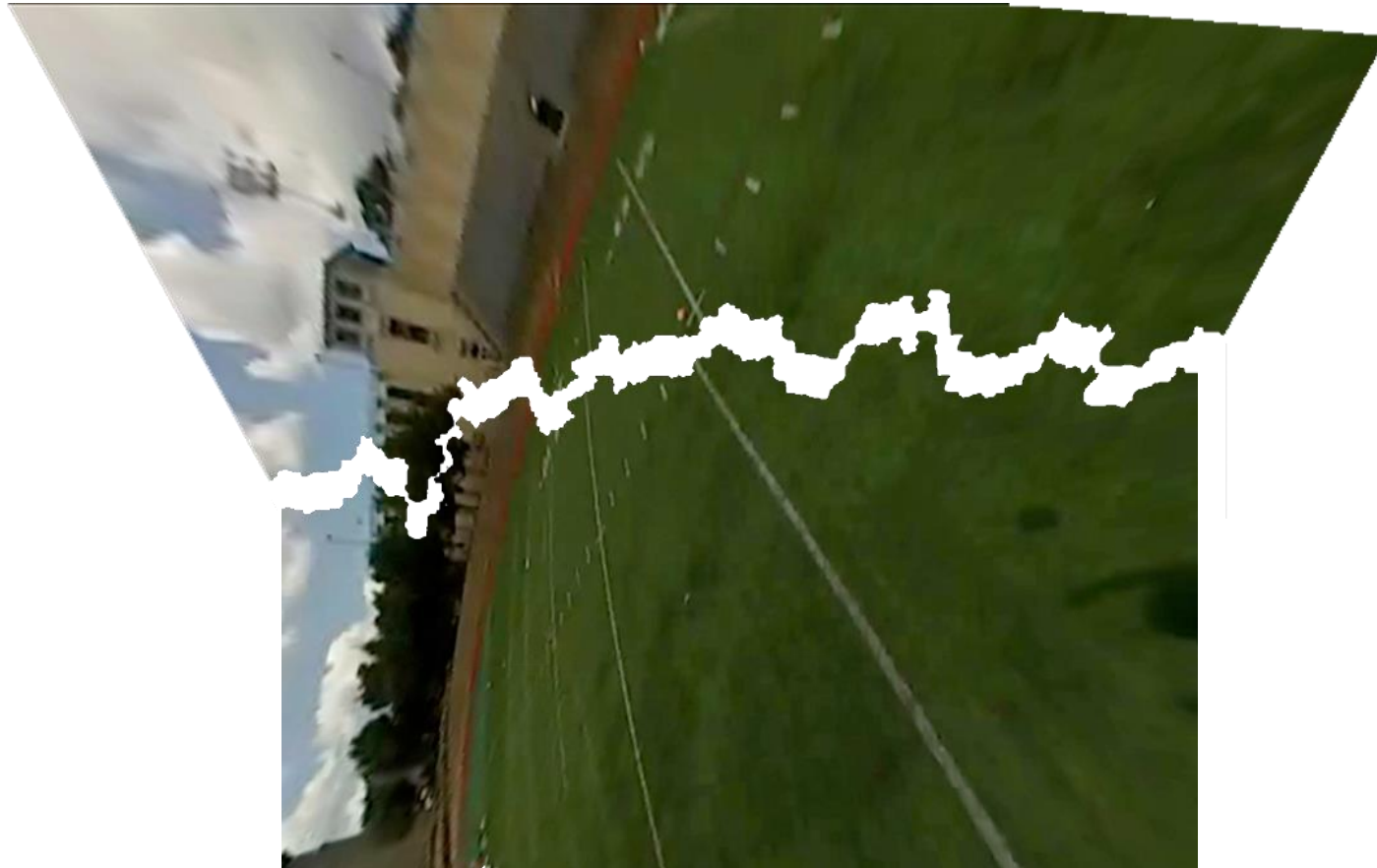


What can we do instead of blending?

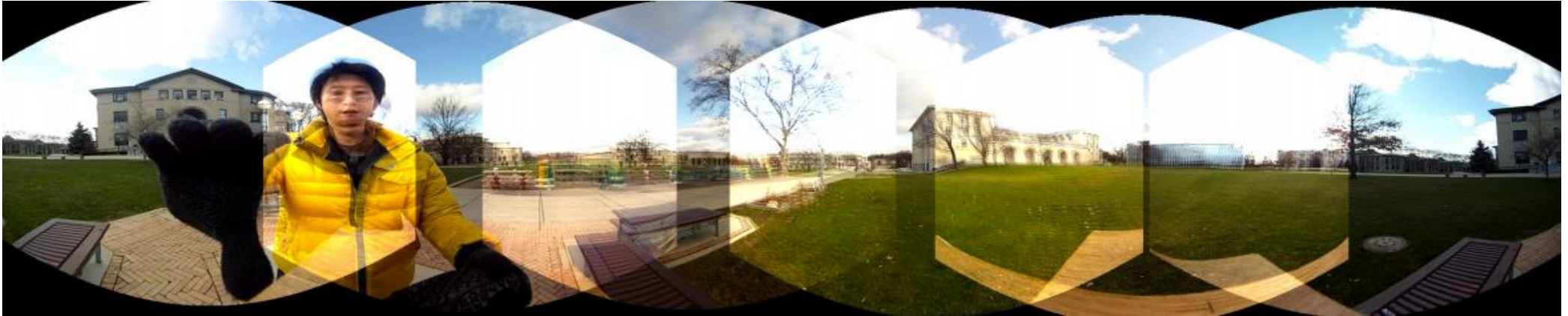
# Seam stitching

Another use for image seam selection:

- instead of blending the images, cut them and stitch them together



# Seam stitching



alpha blending

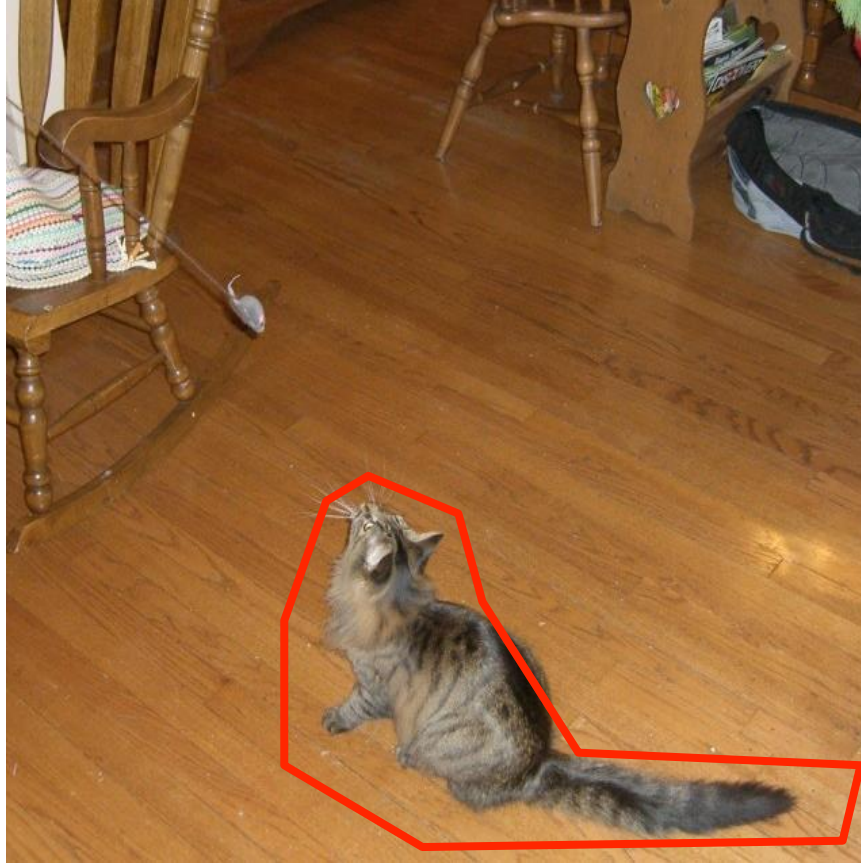


AutoStitch



# Examples

Where will intelligent scissors work well, or have problems?





# Graph-cuts and GrabCut

# GrabCut

Only user input is the box!



Rother et al., "Interactive Foreground Extraction with Iterated Graph Cuts," SIGGRAPH 2004

# Combining region and boundary information

Magic Wand (198?)

Intelligent scissors

GrabCut

user input



result



regions



boundary



regions & boundary

# GrabCut is a mixture of two components

1. Segmentation using graph cuts
2. Foreground-background modeling using unsupervised clustering

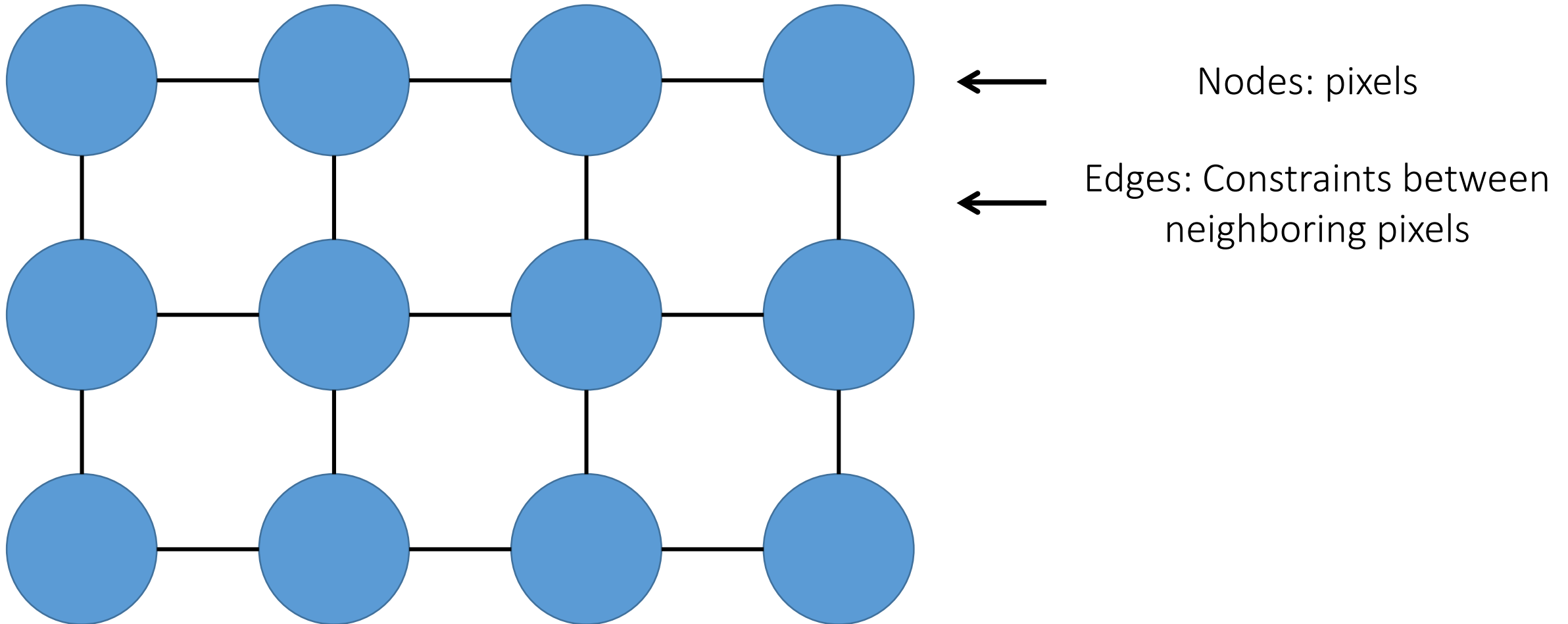
# GrabCut is a mixture of two components

1. Segmentation using graph cuts

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# Segmentation using graph cuts

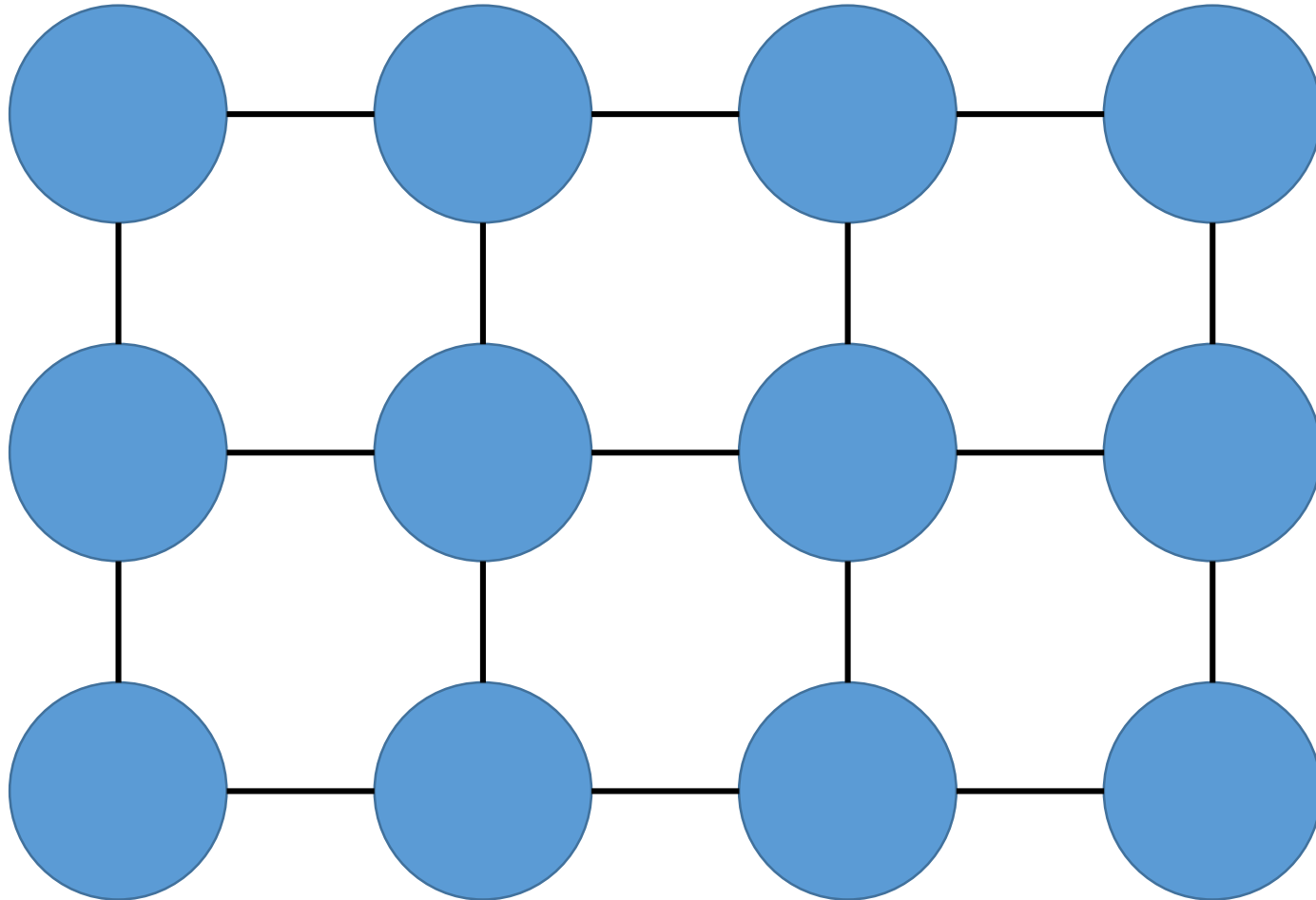
Remember: Graph-based view of images



# Markov Random Field (MRF)

Assign foreground/background labels based on:

$$Energy(\mathbf{y}; \theta, data) = \sum_i \psi_1(y_i; \theta, data) + \sum_{i,j \in edges} \psi_2(y_i, y_j; \theta, data)$$



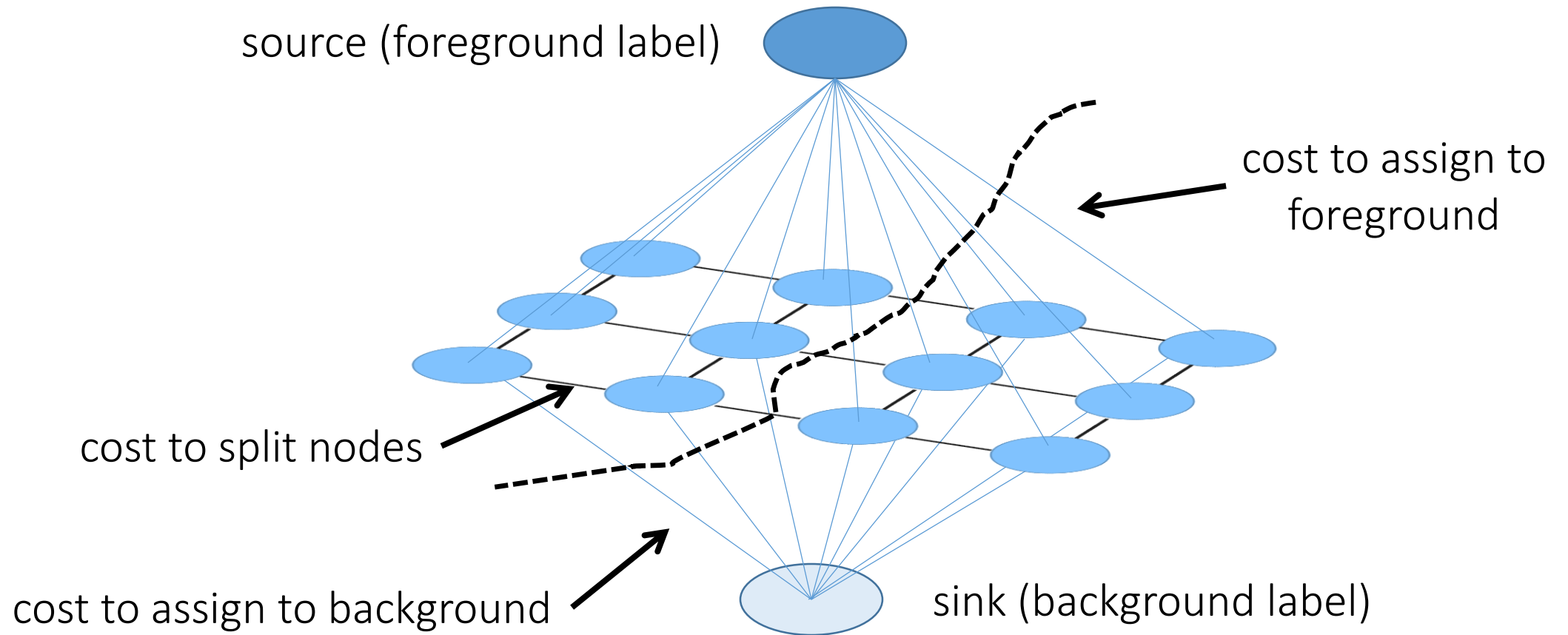
↑  
Given its intensity  
value, how likely is a  
pixel to be foreground  
or background?

↑  
Given their intensity values,  
how likely two neighboring  
pixels to have two labels?

What kind of cost functions  
would you use for GrabCut?

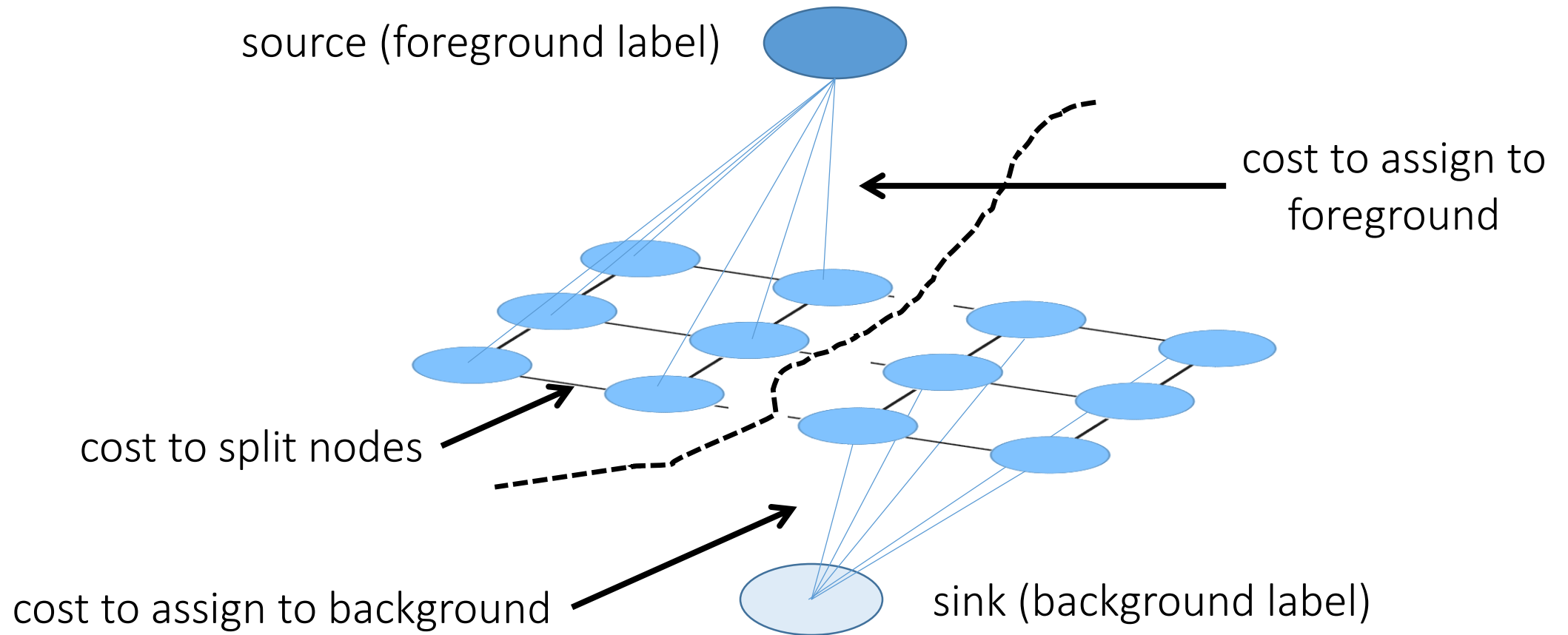


# Solving MRFs using max-flow/min-cuts (graph cuts)



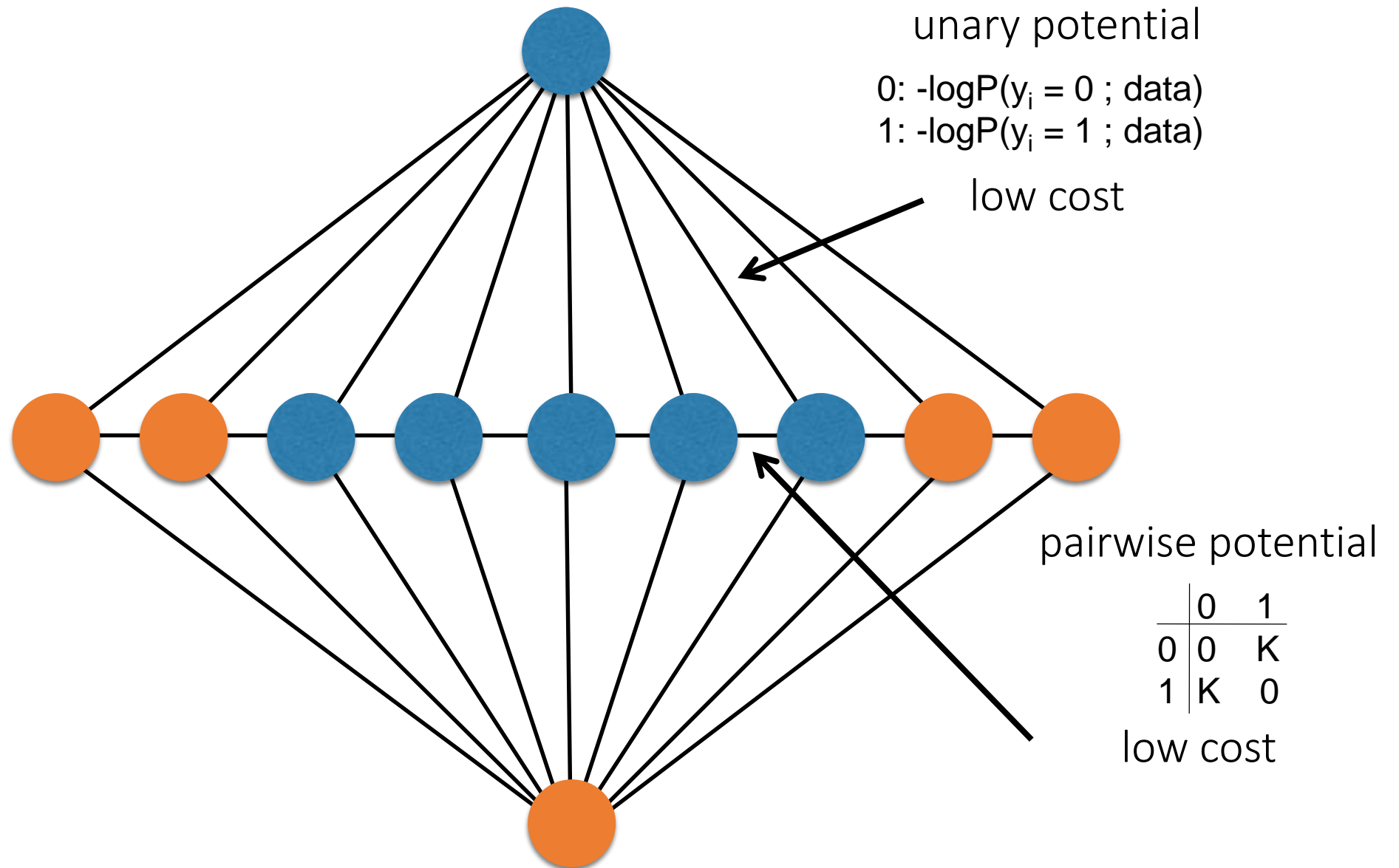
$$Energy(\mathbf{y}; \theta, data) = \sum_i \psi_1(y_i; \theta, data) + \sum_{i,j \in edges} \psi_2(y_i, y_j; \theta, data)$$

# Solving MRFs using max-flow/min-cuts (graph cuts)



$$Energy(\mathbf{y}; \theta, data) = \sum_i \psi_1(y_i; \theta, data) + \sum_{i,j \in edges} \psi_2(y_i, y_j; \theta, data)$$


# A toy visual example



# Graph-cuts segmentation

1. Define graph
  - usually 4-connected or 8-connected
2. Set weights to foreground/background

How would you determine these for GrabCut?


$$unary\_potential(x) = -\log \left( \frac{P(c(x); \theta_{foreground})}{P(c(x); \theta_{background})} \right)$$

3. Set weights for edges between pixels

$$edge\_potential(x, y) = k_1 + k_2 \exp \left\{ \frac{-\|c(x) - c(y)\|^2}{2\sigma^2} \right\}$$

4. GraphCut: Apply min-cut/max-flow algorithm

# GrabCut is a mixture of two components

1. Segmentation using graph cuts

2. Foreground-background modeling using unsupervised clustering

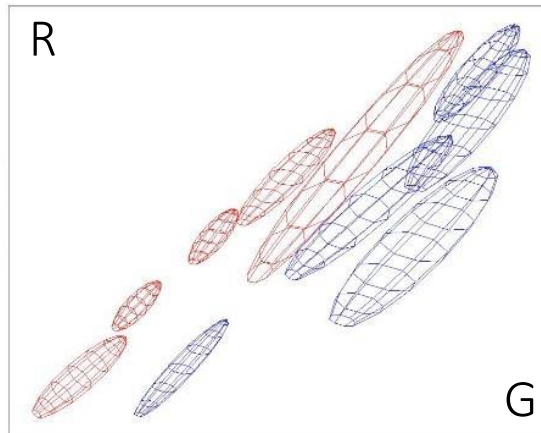
# Foreground-background modeling

Given foreground/background labels



build a color model for both

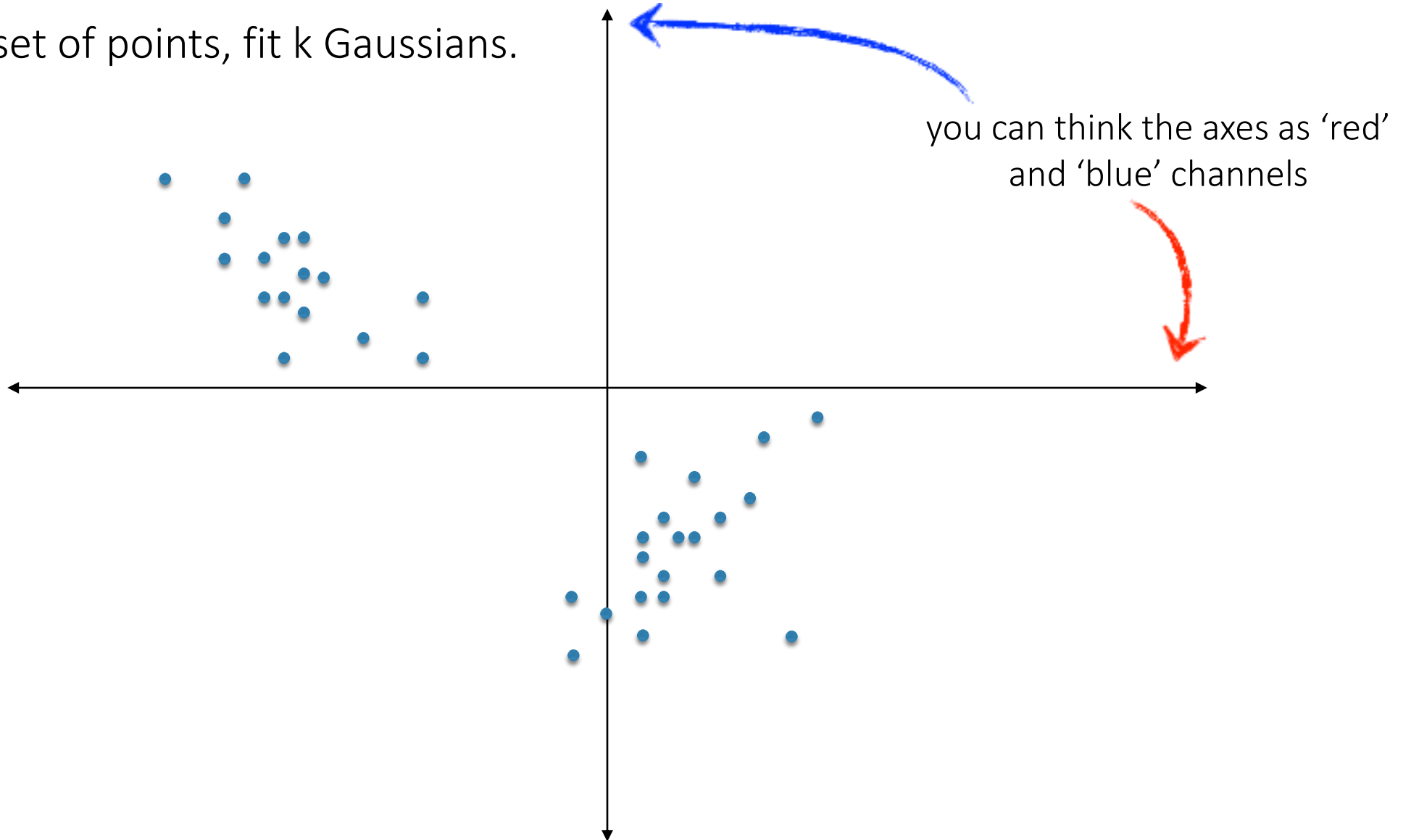
foreground



background

# Learning color models

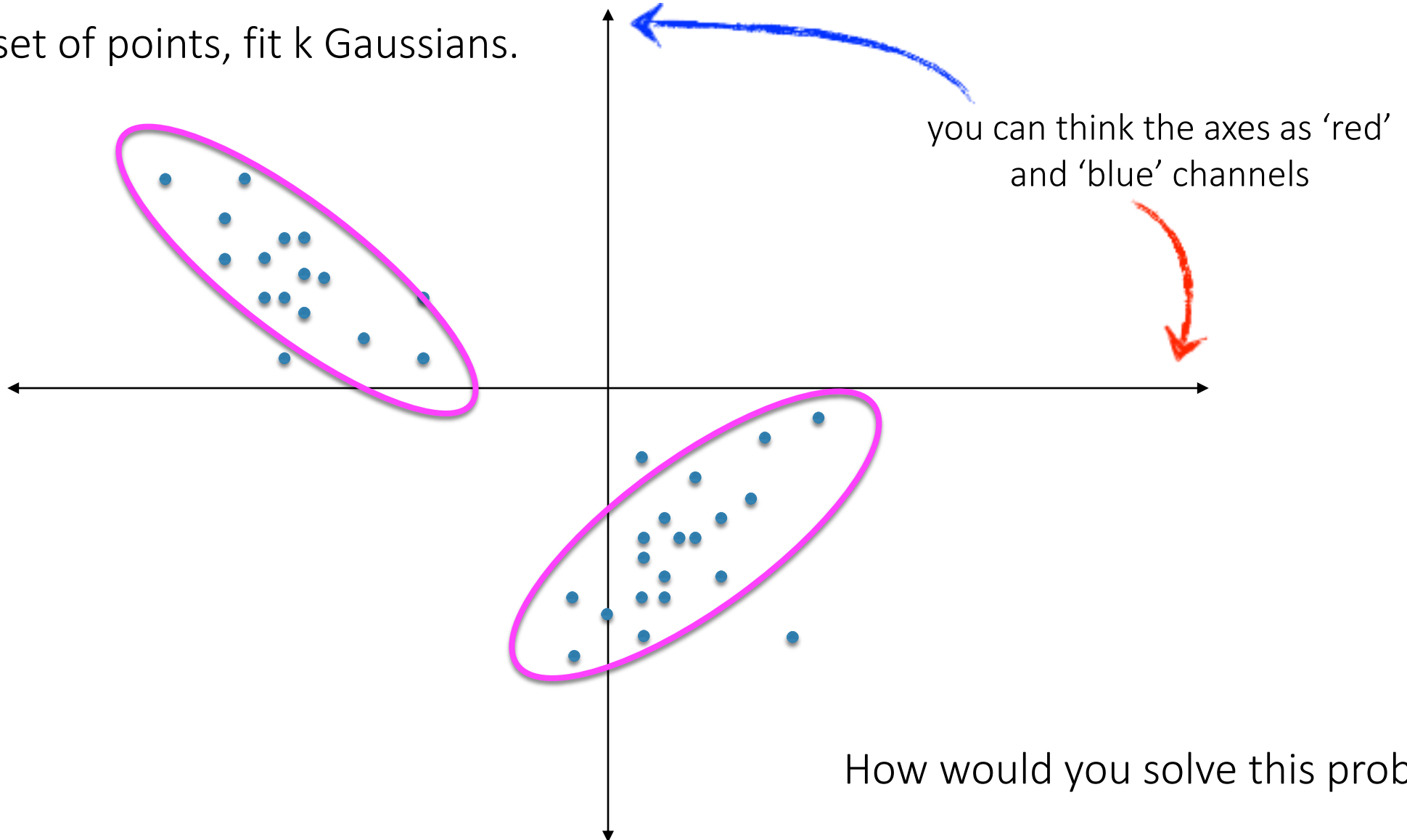
Given a set of points, fit  $k$  Gaussians.





# Learning color models

Given a set of points, fit  $k$  Gaussians.

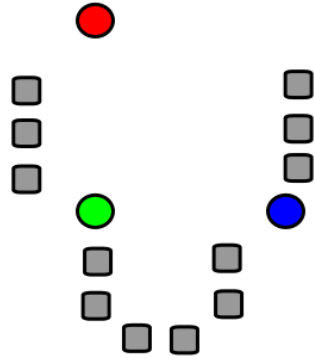


# Intuition: “hard” clustering using K-means

Given  $k$ :

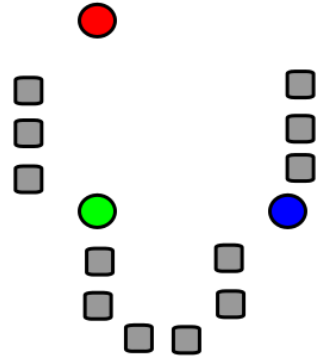
1. Select initial centroids at random.
2. Assign each object to the cluster with the nearest centroid.
3. Compute each centroid as the mean of the objects assigned to it.
4. Repeat previous 2 steps until no change.

# K-means visualization

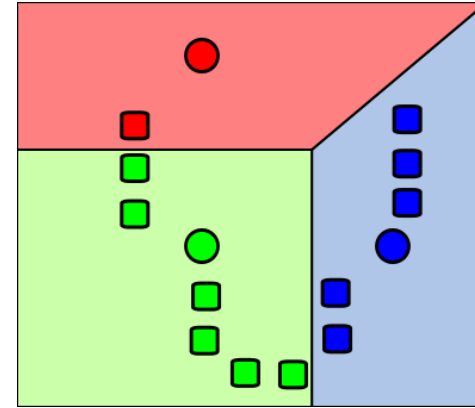


1. Select initial  
centroids at random

# K-means visualization

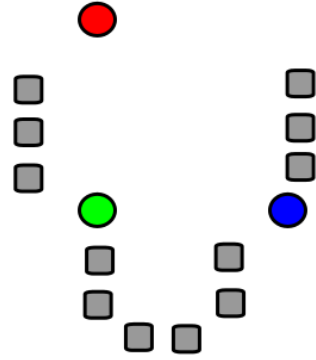


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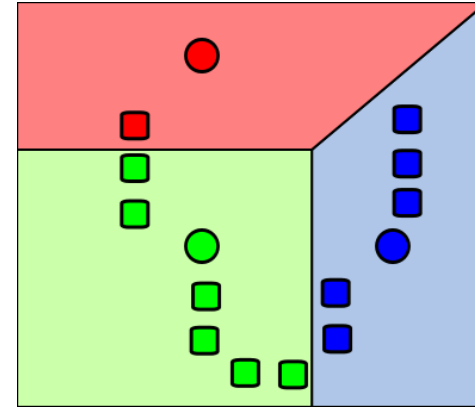


2. Assign each object to the cluster with the nearest centroid.

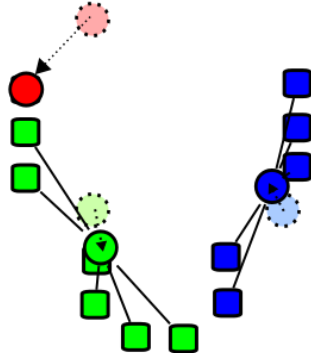
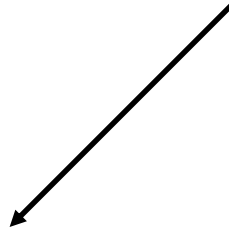
# K-means visualization



1. Select initial centroids at random



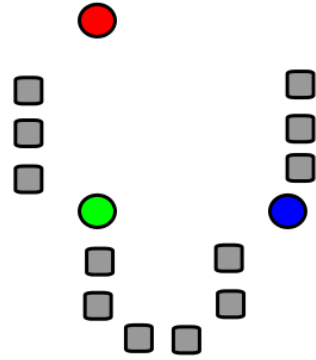
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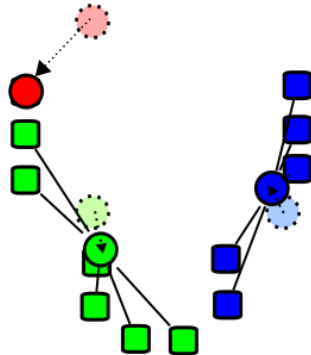
3. Compute each centroid as the mean of the objects assigned to it (go to 2)



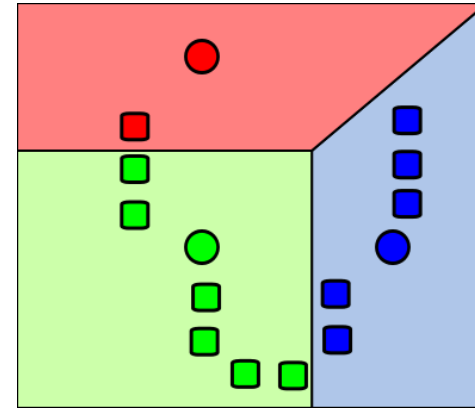
# K-means visualization



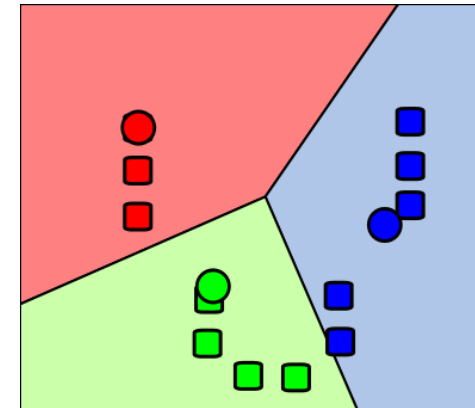
1. Select initial centroids at random



3. Compute each centroid as the mean of the objects assigned to it (go to 2)



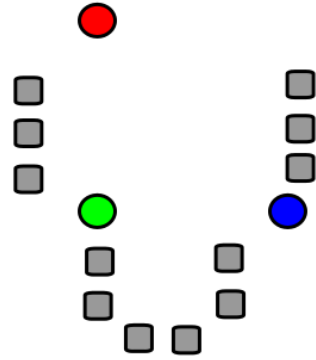
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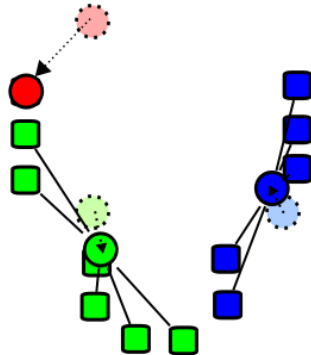
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Repeat previous 2 steps until no change

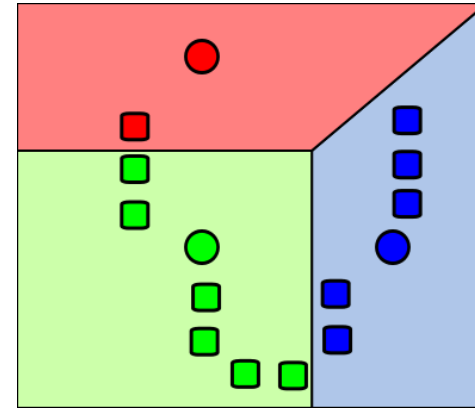
# K-means visualization



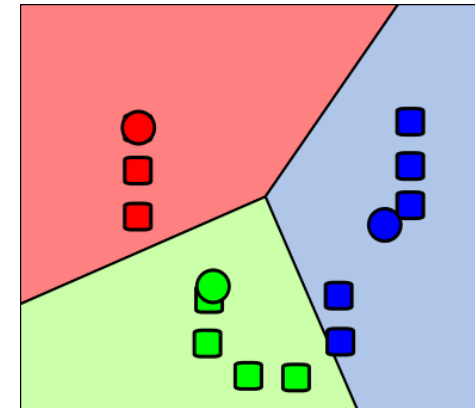
1. Select initial centroids at random



3. Compute each centroid as the mean of the objects assigned to it (go to 2)



2. Assign each object to the cluster with the nearest centroid.



2. Assign each object to the cluster with the nearest centroid.

# Expectation-Maximization: “soft” version of K-means

Given  $k$ :

1. Select initial centroids at random.

compute the probability of each object being in a cluster

E-step

2. Assign each object to the cluster with the nearest centroid.

and covariance

M-step

3. Compute each centroid as the mean of the objects assigned to it.

weighed by the probability of being in that cluster

4. Repeat previous 2 steps until no change.

# Unsupervised clustering

Model: **Mixture of Gaussians**

Algorithm: **Expectation Maximization**

E step  $Q(\boldsymbol{\theta}|\boldsymbol{\theta}^{(t)}) = \mathbb{E}_{\mathbf{Z}|\mathbf{X},\boldsymbol{\theta}^{(t)}} [\log L(\boldsymbol{\theta}; \mathbf{X}, \mathbf{Z})]$  Compute the expected log-likelihood

M step  $\boldsymbol{\theta}^{(t+1)} = \arg \max_{\boldsymbol{\theta}} Q(\boldsymbol{\theta}|\boldsymbol{\theta}^{(t)})$  Update parameters based on likelihood

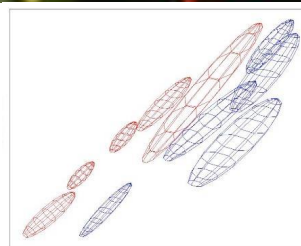
Important result for GrabCut:

we can compute the **likelihood** of a **pixel** belonging to the **foreground** or **background** as:

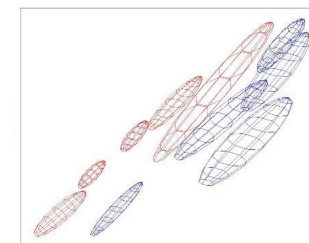
$$p(c(x); \boldsymbol{\theta}) = \prod_{k=1}^K \alpha_k \cdot \mathcal{N}(c(x); \boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k)$$

# GrabCut is a mixture of two components

1. Segmentation using graph cuts
  - Requires having foreground model



2. Foreground-background modeling using unsupervised clustering
  - Requires having segmentation

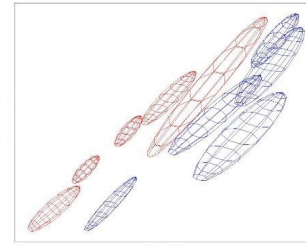


What do we do?

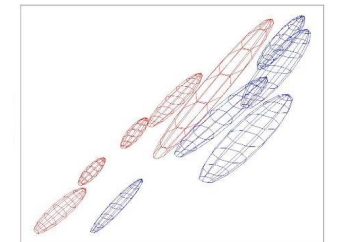


# GrabCut: iterate between two steps

1. Segmentation using graph cuts
  - Requires having foreground model

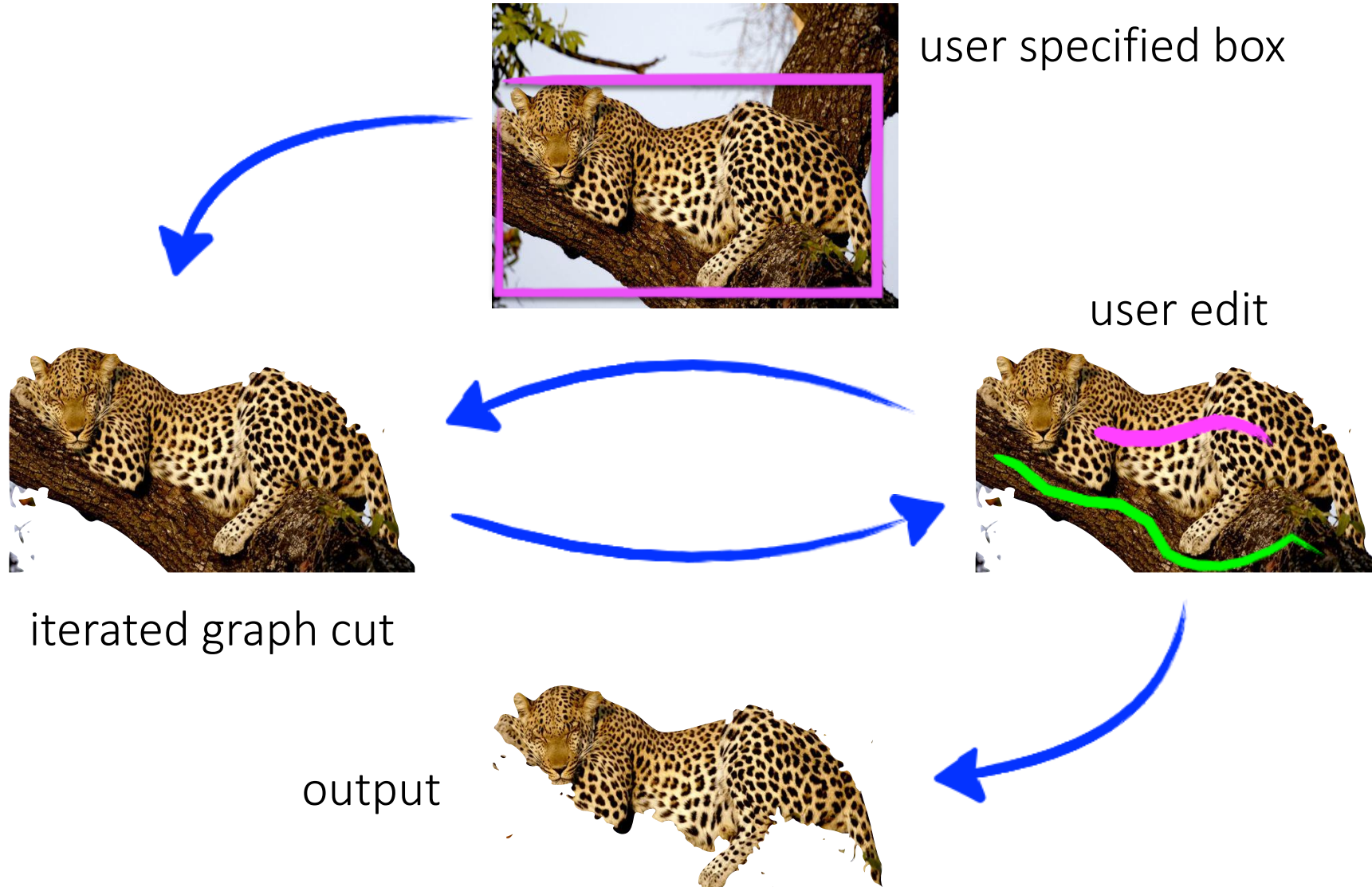


2. Foreground-background modeling using unsupervised clustering
  - Requires having segmentation



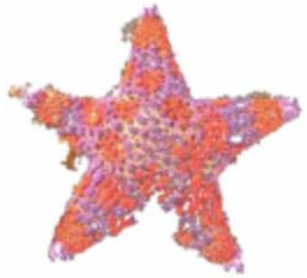
What do we do?

# Iteration can be interactive

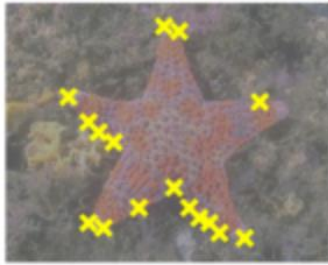


# Examples

Magic Wand



Magnetic Lasso



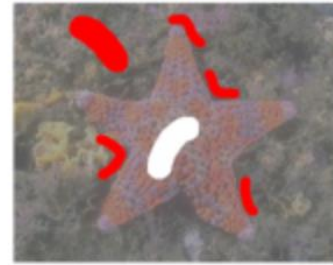
Knockout 2



Bayes Matte



BJ – Graph Cut

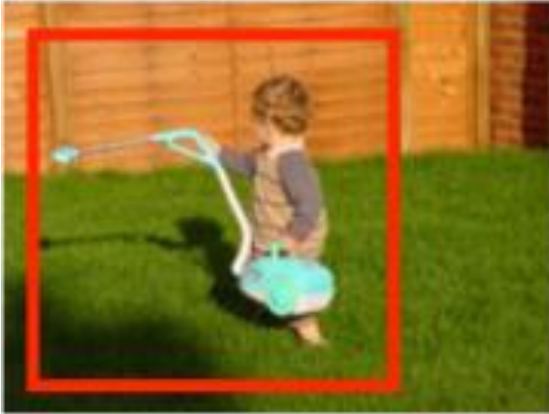


GrabCut



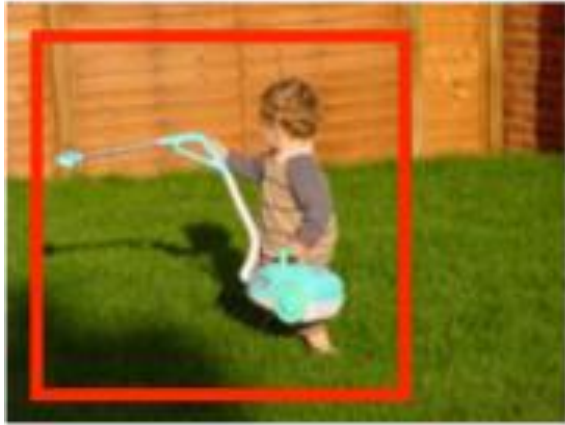


# Examples



What is easy or hard about these cases for graph cut-based segmentation?

# Examples





# Examples



# Examples



Lazy Snapping  
[Li et al. SIGGRAPH 2004]



# Graph-cuts are a very general, very useful tool

- denoising
- stereo
- texture synthesis
- segmentation
- classification
- recognition
- ...



**3D model of  
scene**

Some notes about cutting-and-pasting

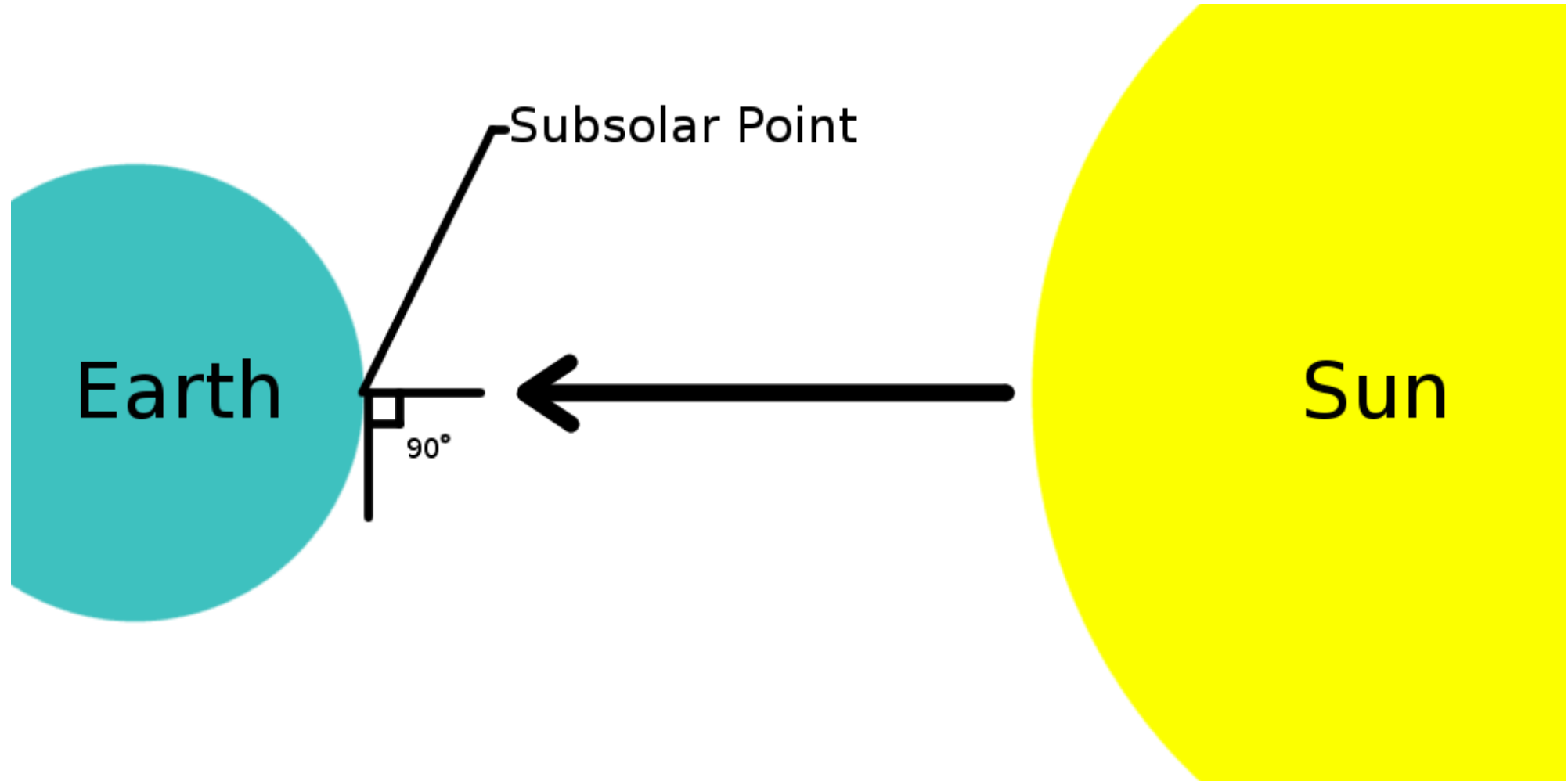


# Real or composite, and why?





Real: Lahaina noon (or noon at subsolar point)



Real or composite, and why?



# Composite: Inconsistent shadows



# Composite: Inconsistent shadows



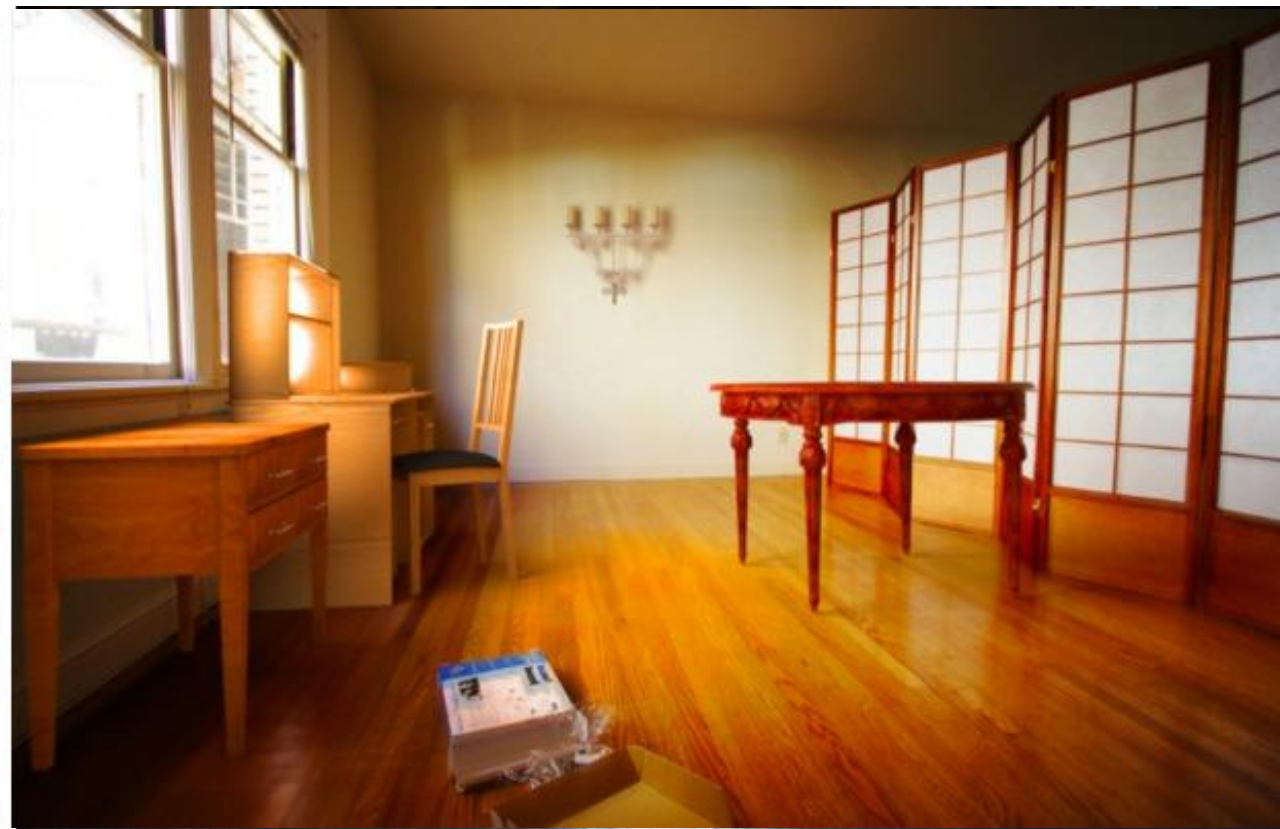
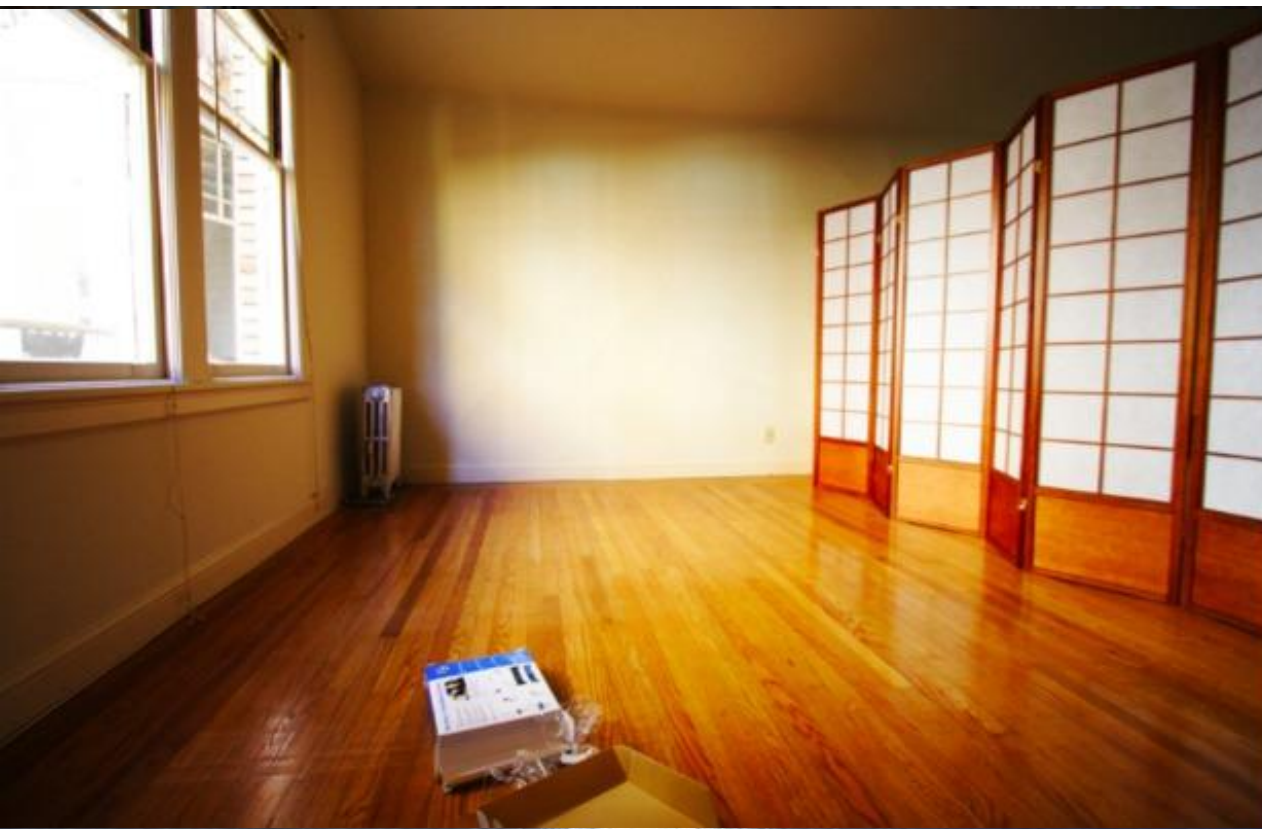
Fig. 1. Our algorithm finds that the shadows in this 1969 moon landing photo are physically consistent with a single light source. The solid lines correspond to constraints from cast shadows and dashed lines correspond to constraints from attached shadows. The region outlined in black, which extends beyond the figure boundary, contains the projected light locations that satisfy all of these constraints.

Original image copyright 1969, NASA

Kee et al., "Exposing Photo Manipulation with Inconsistent Shadows," ToG 2014



# Photorealistic compositing



Karsch et al., "Rendering Synthetic Objects into Legacy Photographs," SIGGRAPH Asia 2011



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Karsch et al., "Rendering Synthetic Objects into Legacy Photographs," SIGGRAPH Asia 2011

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# Photorealistic compositing



Karsch et al., "Rendering Synthetic Objects into Legacy Photographs," SIGGRAPH Asia 2011

# Photorealistic compositing

How would you do this?



# References

Basic reading:

- Szeliski textbook, Sections 5.1.3, 5.3.1, 9.3.2, 9.3.3, 10.4.3.
- Mortensen and Barrett, “Intelligent scissors for image composition,” SIGGRAPH 1995.  
the intelligent scissors paper.
- Kwatra et al., Graphcut Textures: Image and Video Synthesis using Graph Cuts, SIGGRAPH 2003.  
the seam collaging paper.
- Rother et al., “Interactive Foreground Extraction with Iterated Graph Cuts,” SIGGRAPH 2004.  
the GrabCut paper.
- Avidan and Shamir, “Seam Carving for Content-aware Image Resizing,” SIGGRAPH 2007.  
the seam carving paper.

Additional reading:

- Li et al., “Lazy Snapping,” SIGGRAPH 2004.  
a popular variant of GrabCut.
- Felzenszwalb and Zabih, “Dynamic Programming and Graph Algorithms in Computer Vision,” PAMI 2010.  
a great review of graph-based techniques, including shortest path and graph-cut, in computer vision.
- Kee et al., “Exposing photo manipulation with inconsistent shadows,” ToG 2013.  
the paper demonstrating how image forgeries can be detecting by reasoning about the physical accuracy of shadows in an image.
- Karsch et al., “Rendering synthetic objects into legacy photographs”, SIGGRAPH 2011.  
the paper where the photorealistic compositing examples came from.